

# From Model-Based Design to Formal Verification of Adaptive Embedded Systems

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# Self-Adaptive Systems

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# Self-Adaptive Systems

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HW - Fault  
SW - Fault



# Self-Adaptive Systems

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HW - Fault  
SW - Fault

Runtime  
adaptation

# Self-Adaptive Systems

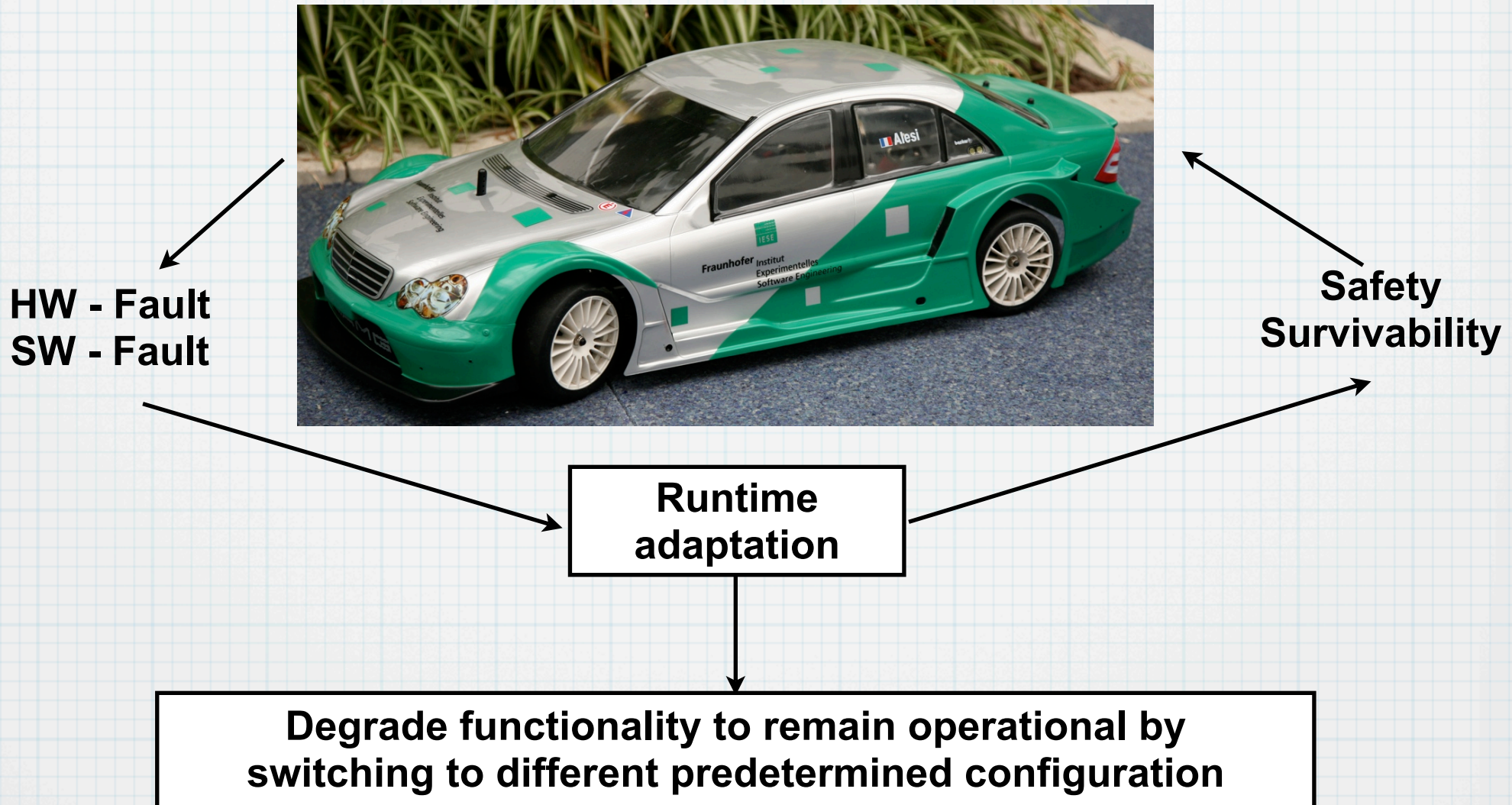
HW - Fault  
SW - Fault



Runtime  
adaptation

Degrade functionality to remain operational by  
switching to different predetermined configuration

# Self-Adaptive Systems



# Adaptive Systems Development

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**Adaptation increases design complexity, since**

- \* decentralized adaptation mechanism**
- \* reconfiguration triggers reconfiguration**
- \* complex interdependencies**

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- \* complex interdependencies

**Solution:**

- \* **Model-Based Design of Adaptive Systems**
- \* **Integrated with Formal Verification of Adaptation Behaviour**

# Integration - Outline

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**Modelling  
Concepts for  
Adaptive  
Systems**

# Integration - Outline

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**Modelling  
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**Verification  
Tools**

**System  
Properties**

# Integration - Outline

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**Modelling  
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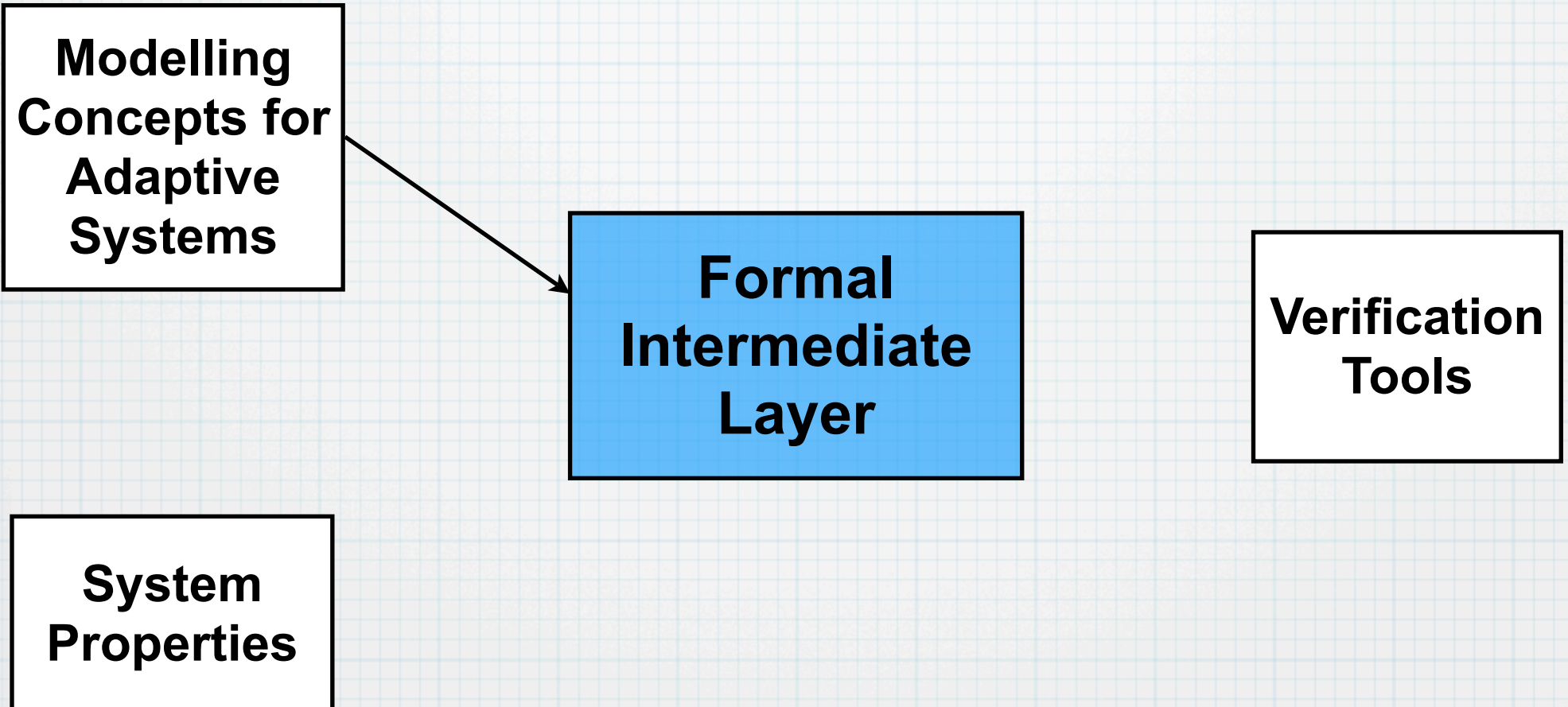
**Formal  
Intermediate  
Layer**

**Verification  
Tools**

**System  
Properties**

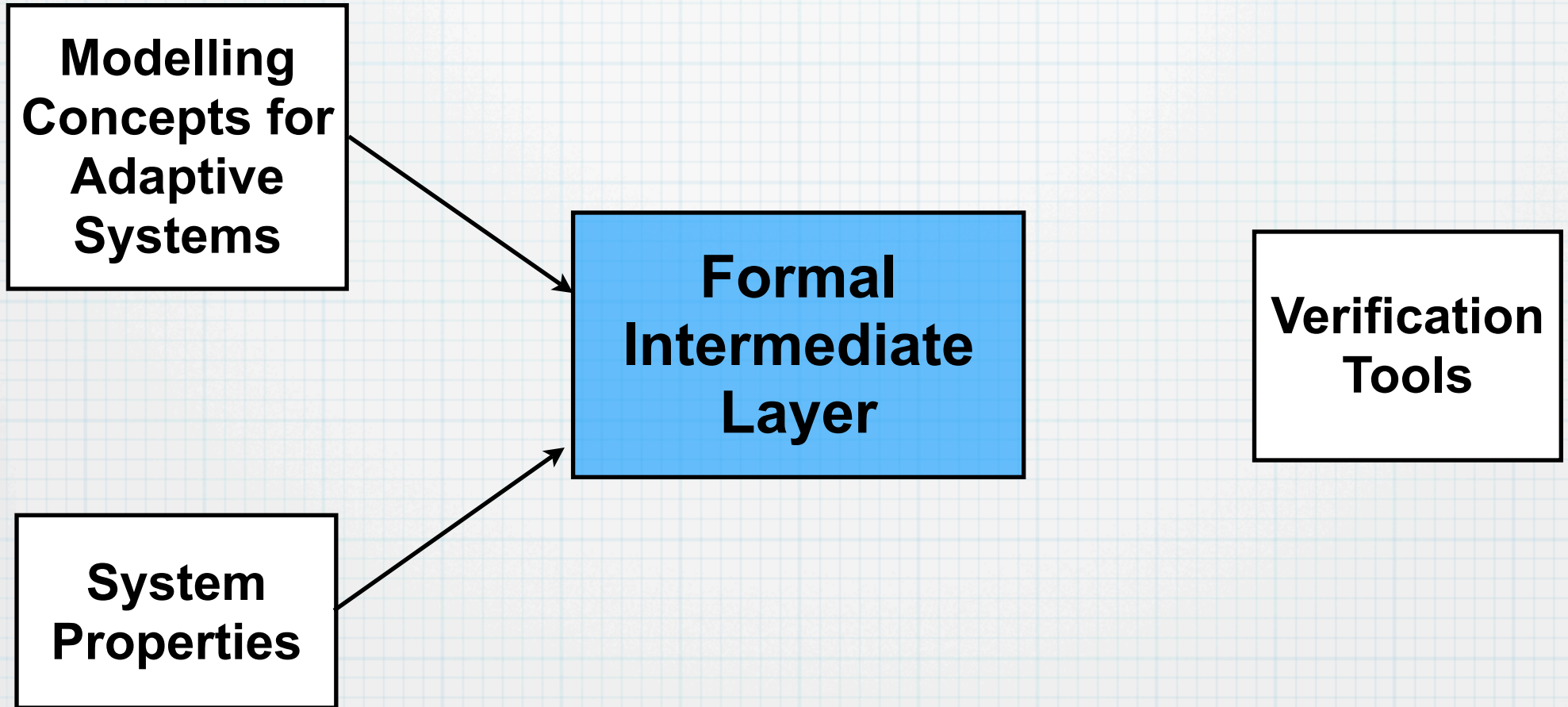
# Integration - Outline

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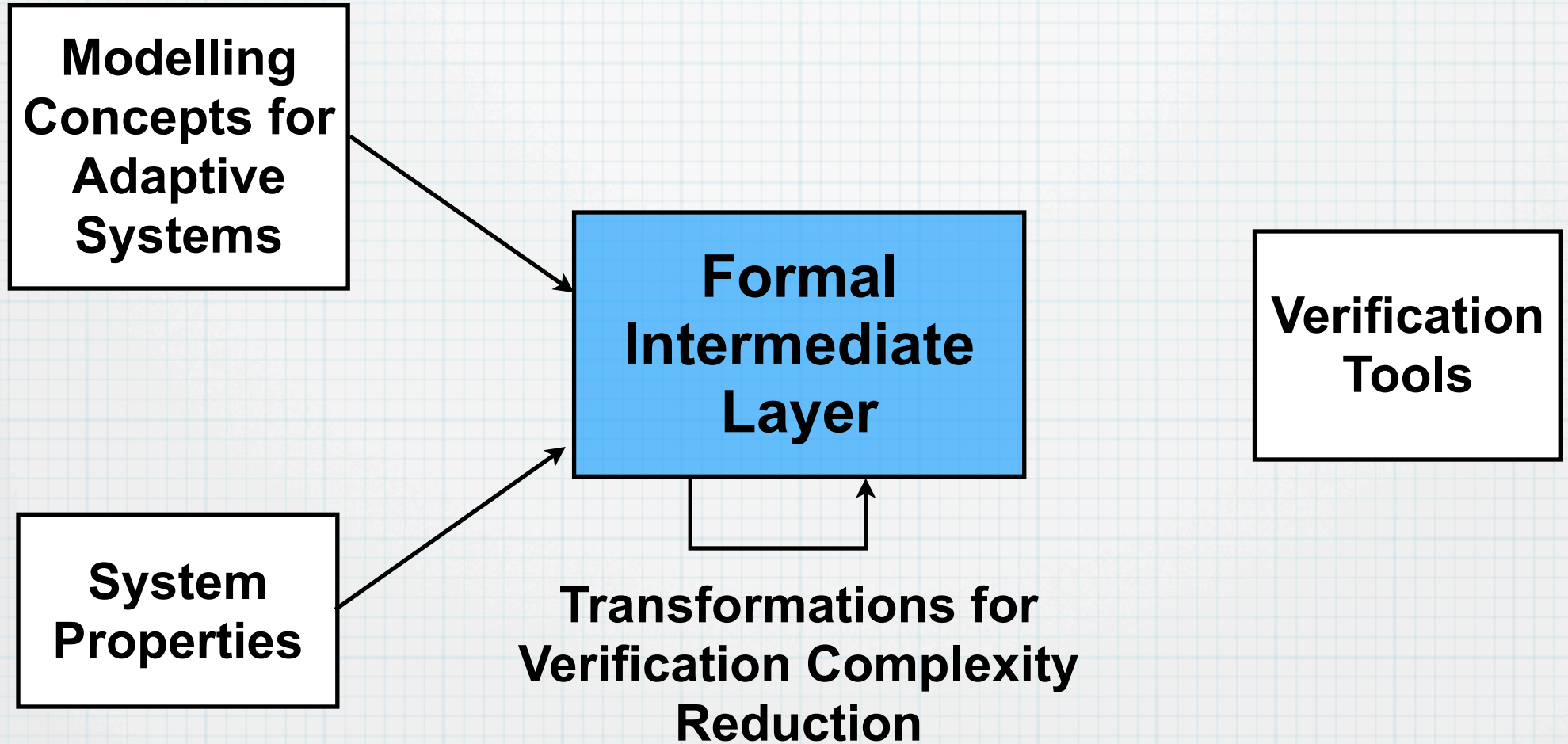
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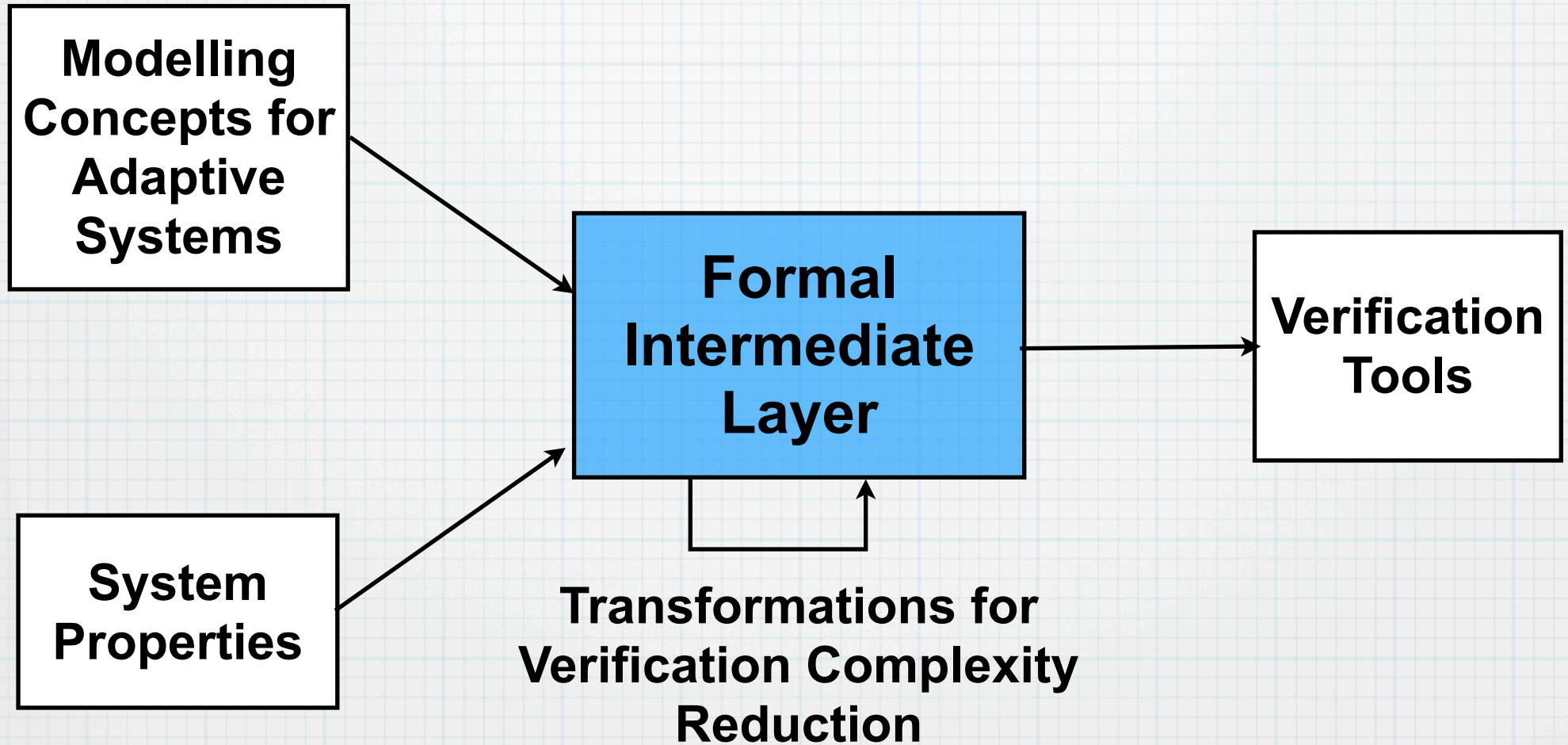
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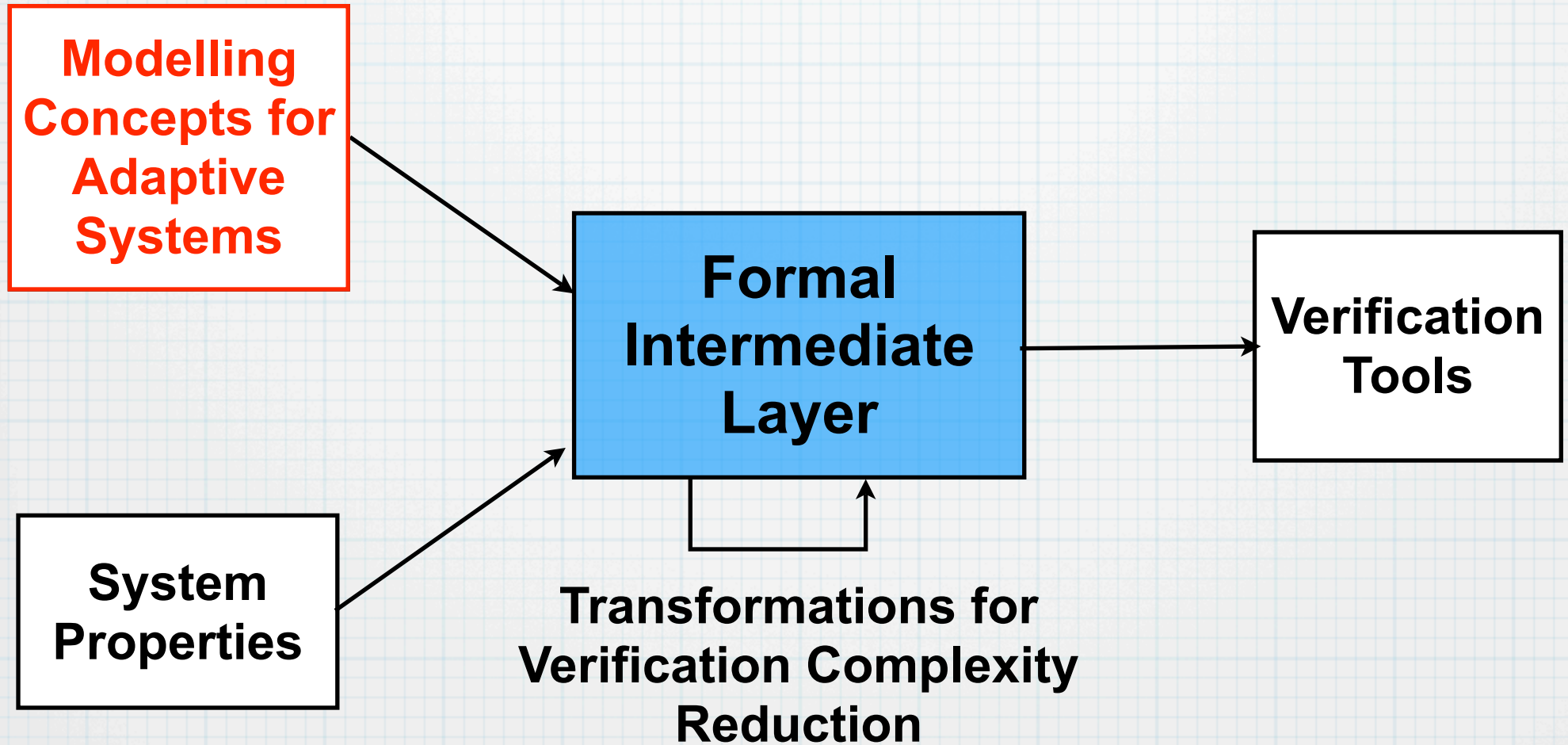
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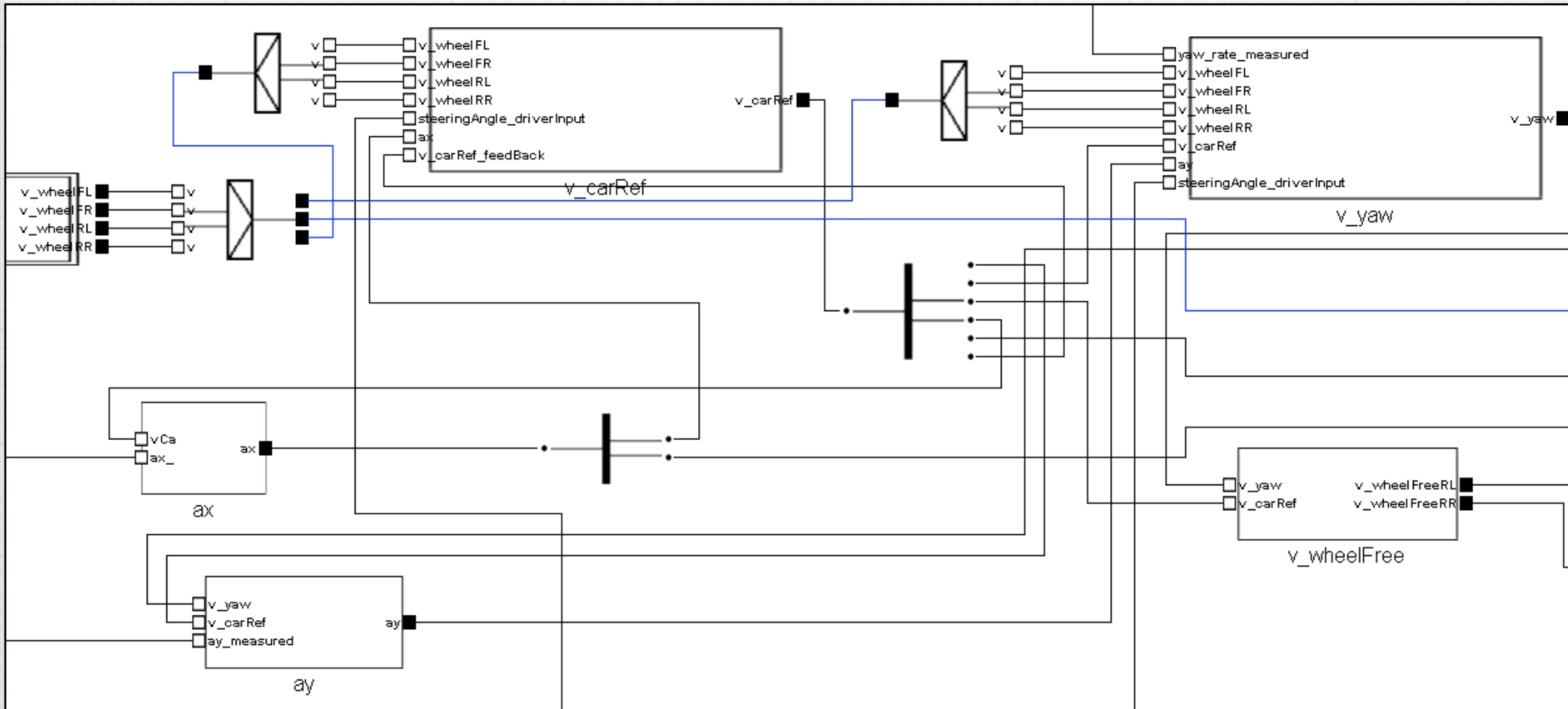


# Adaptive System Modelling (MARS)

## **Main Concepts reducing Design Complexity:**

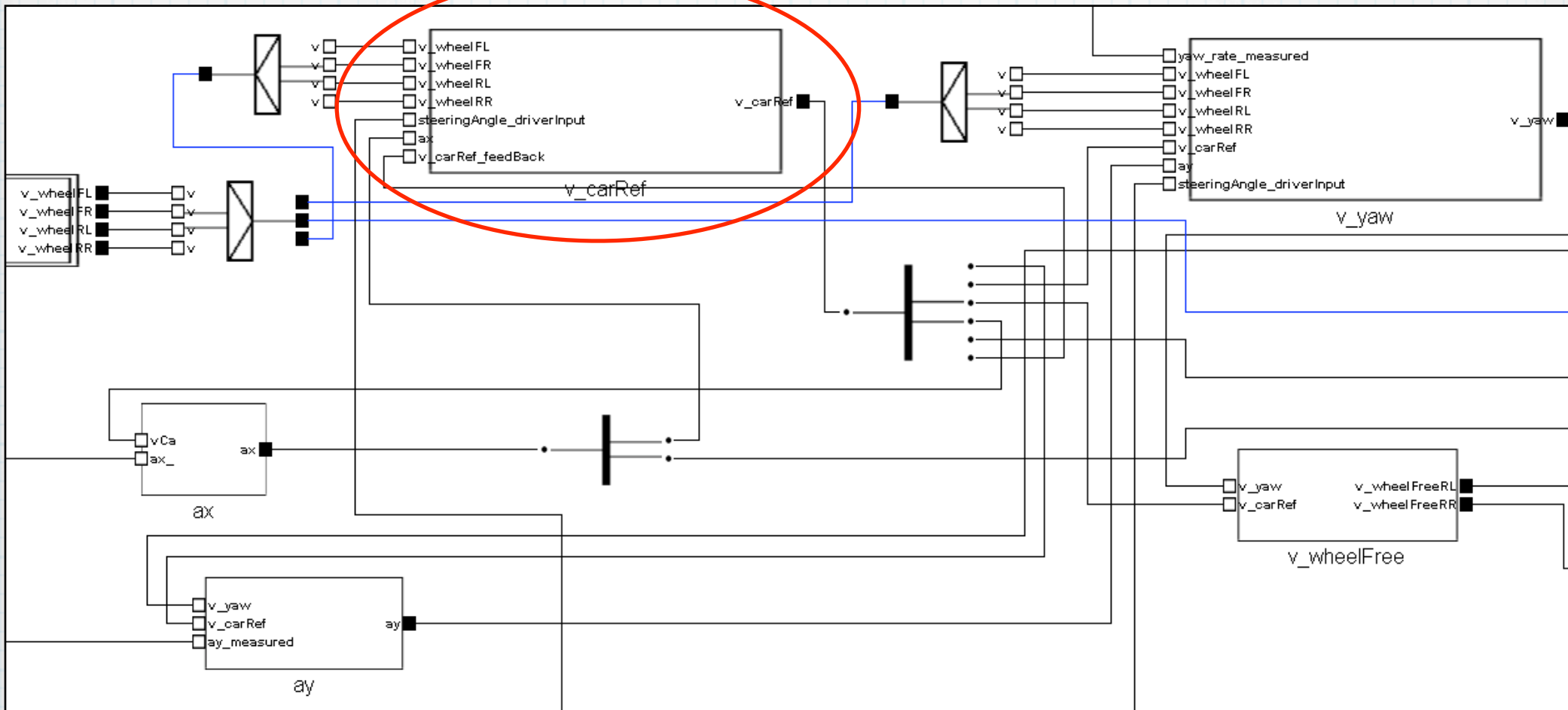
- \* Modular System Structure**
- \* Separation of Adaptation and Functionality in Modules**
- \* Propagation of Adaptation by Qualities attached to Data**

# Modular System Structure



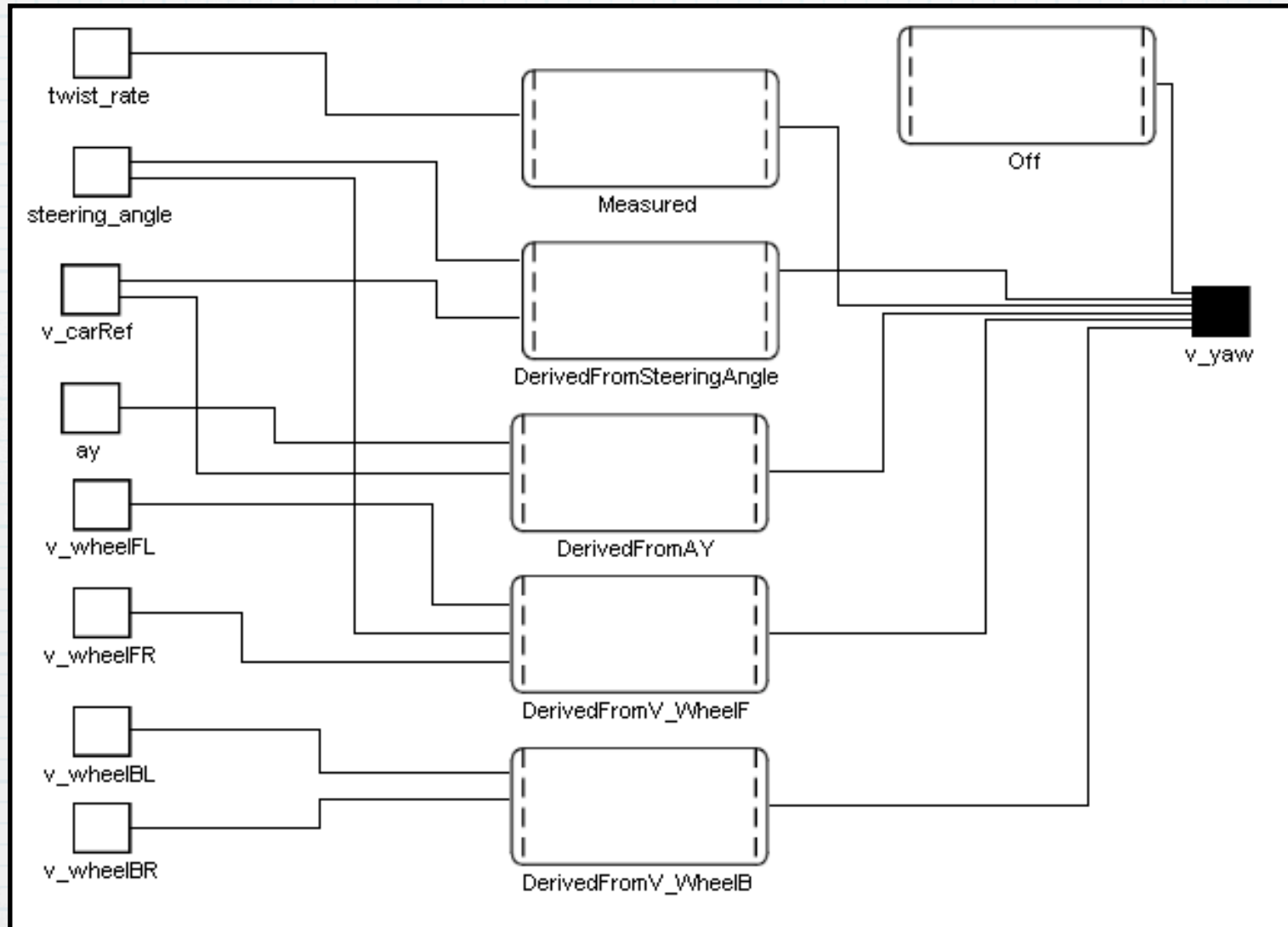
# Modular System Structure

## Module



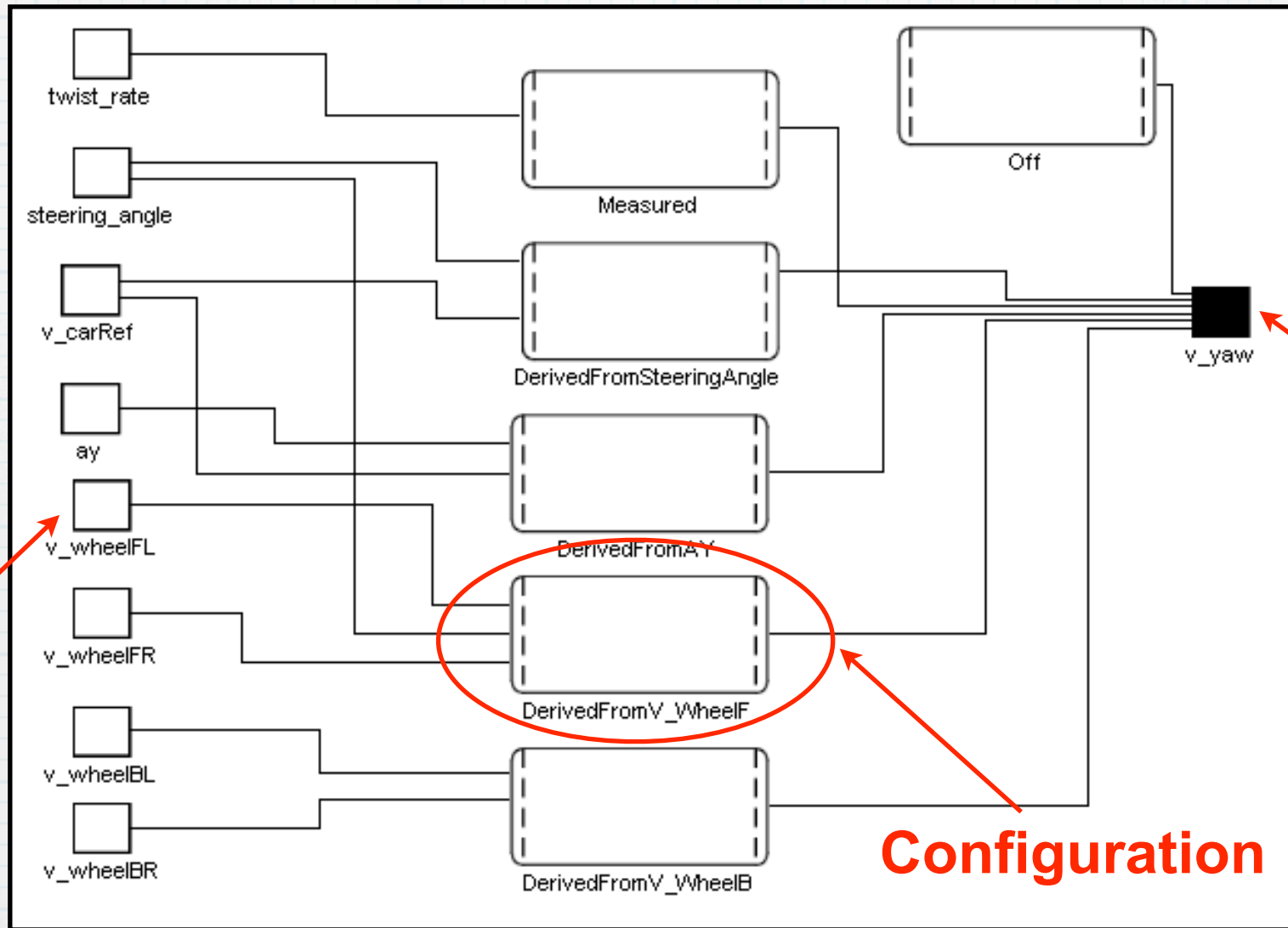
# Adaptive MARS Modules

## Example: Yaw Rate Module



# Adaptive MARS Modules

## Example: Yaw Rate Module

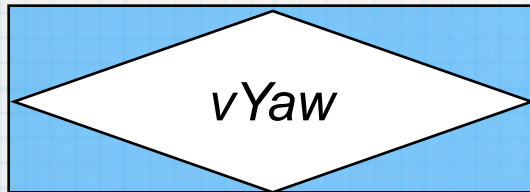


Input

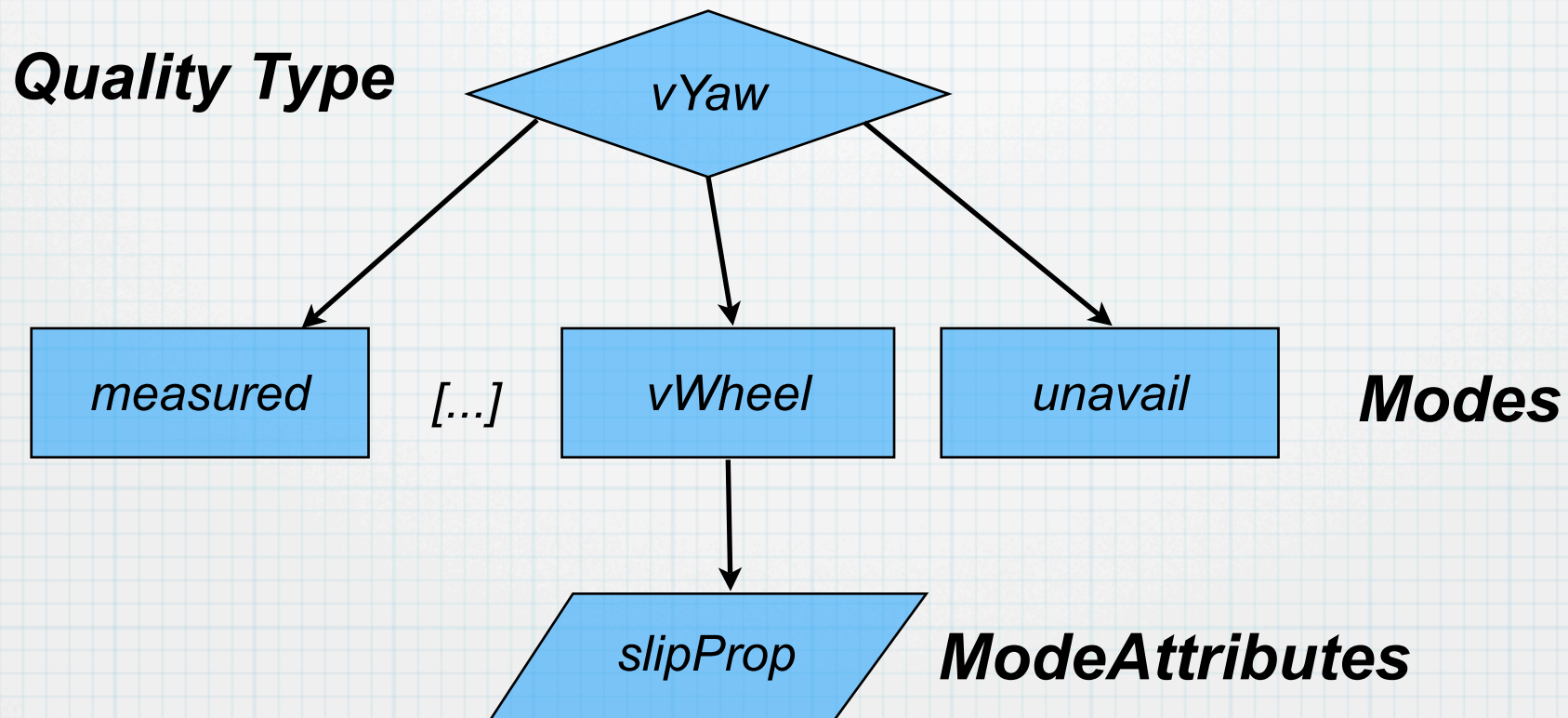
Output

Configuration

# Adaptation Behaviour - Qualities



Quality-Extended Datatypes for Adaptive Systems  
*Dative = [ data type, quality type ]*



# Modelling Adaptation

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# Modelling Adaptation

Adaptation Sequence Chart

Environment

yaw\_rate

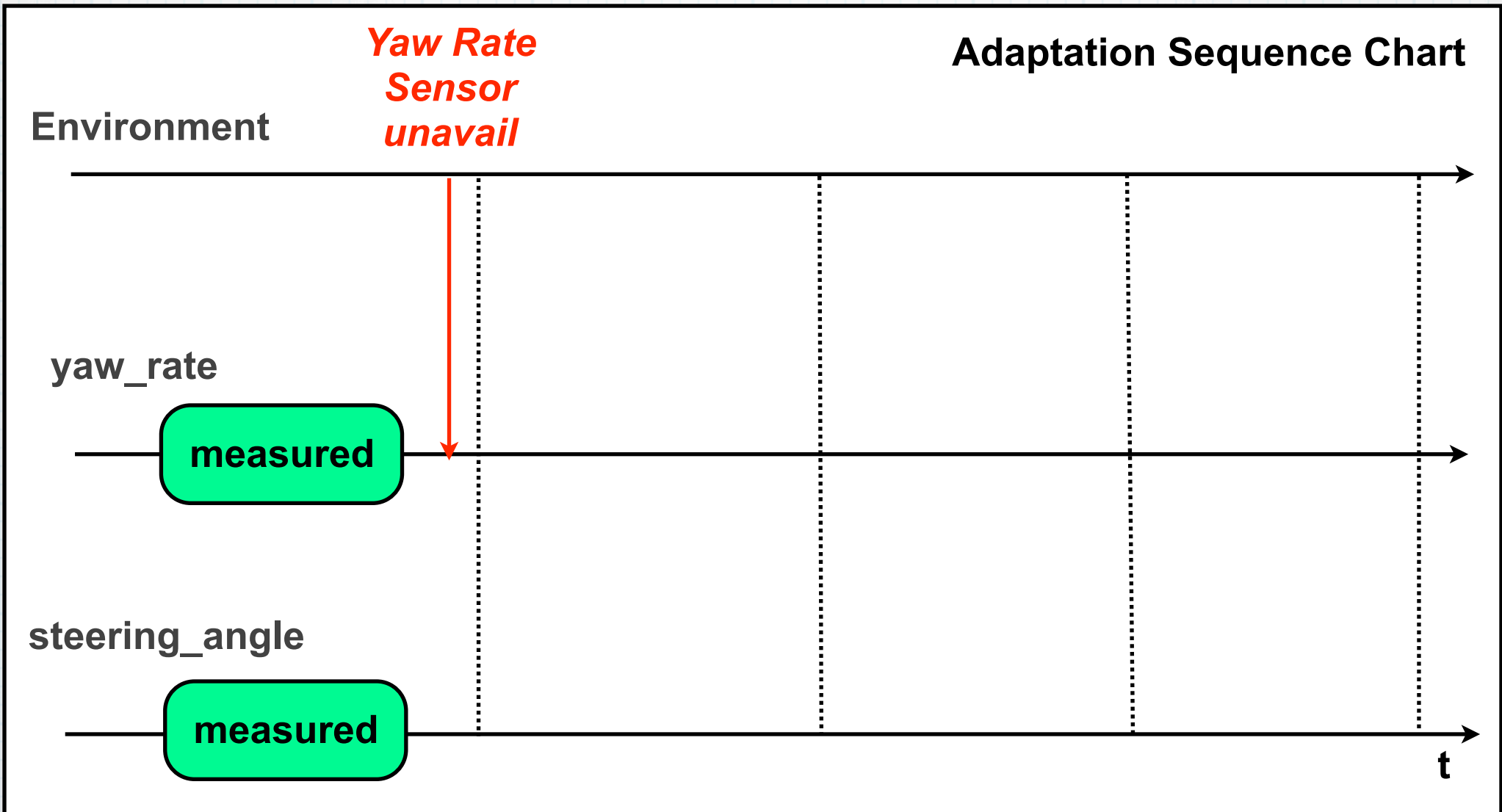
measured

steering\_angle

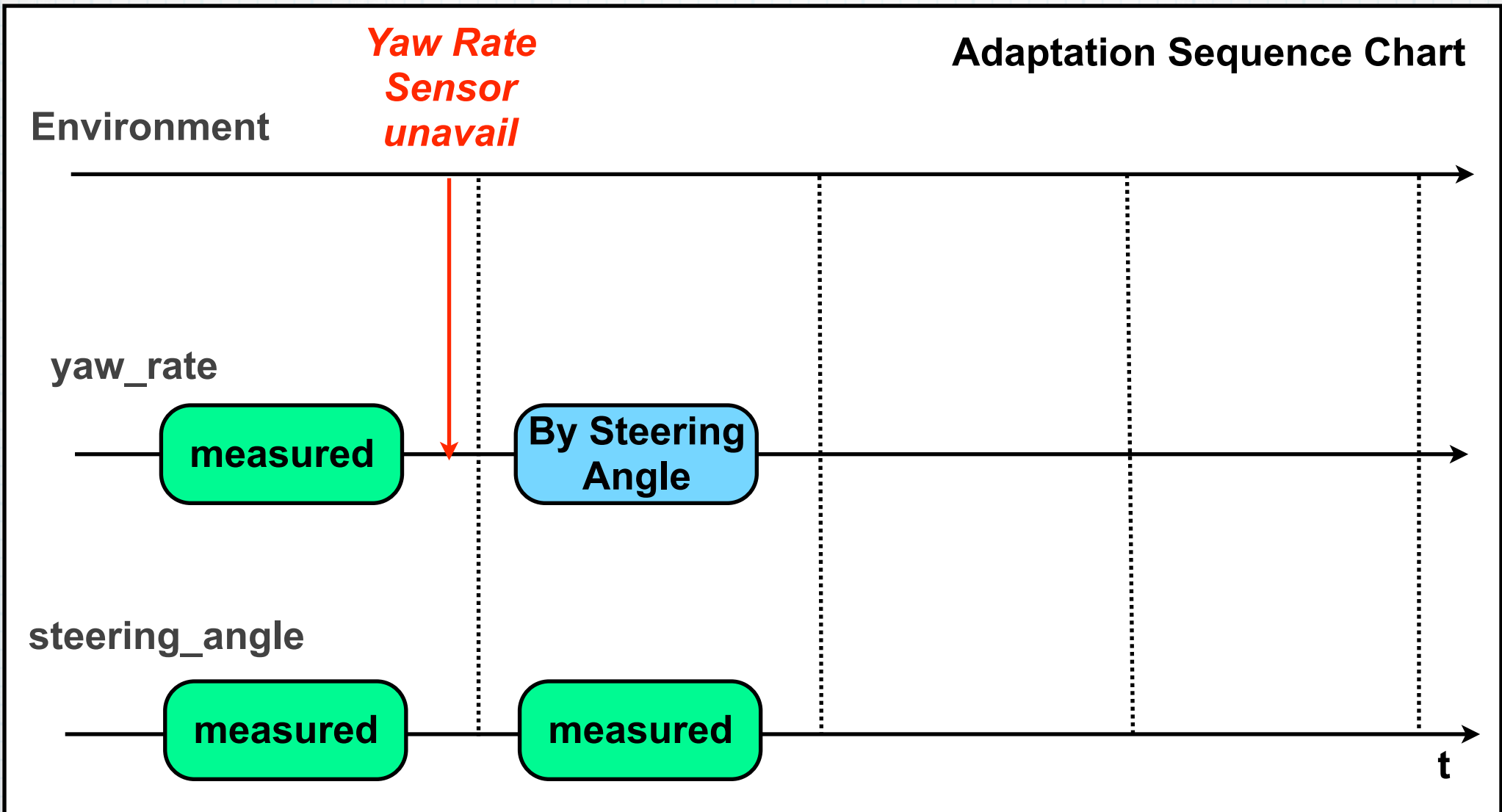
measured

t

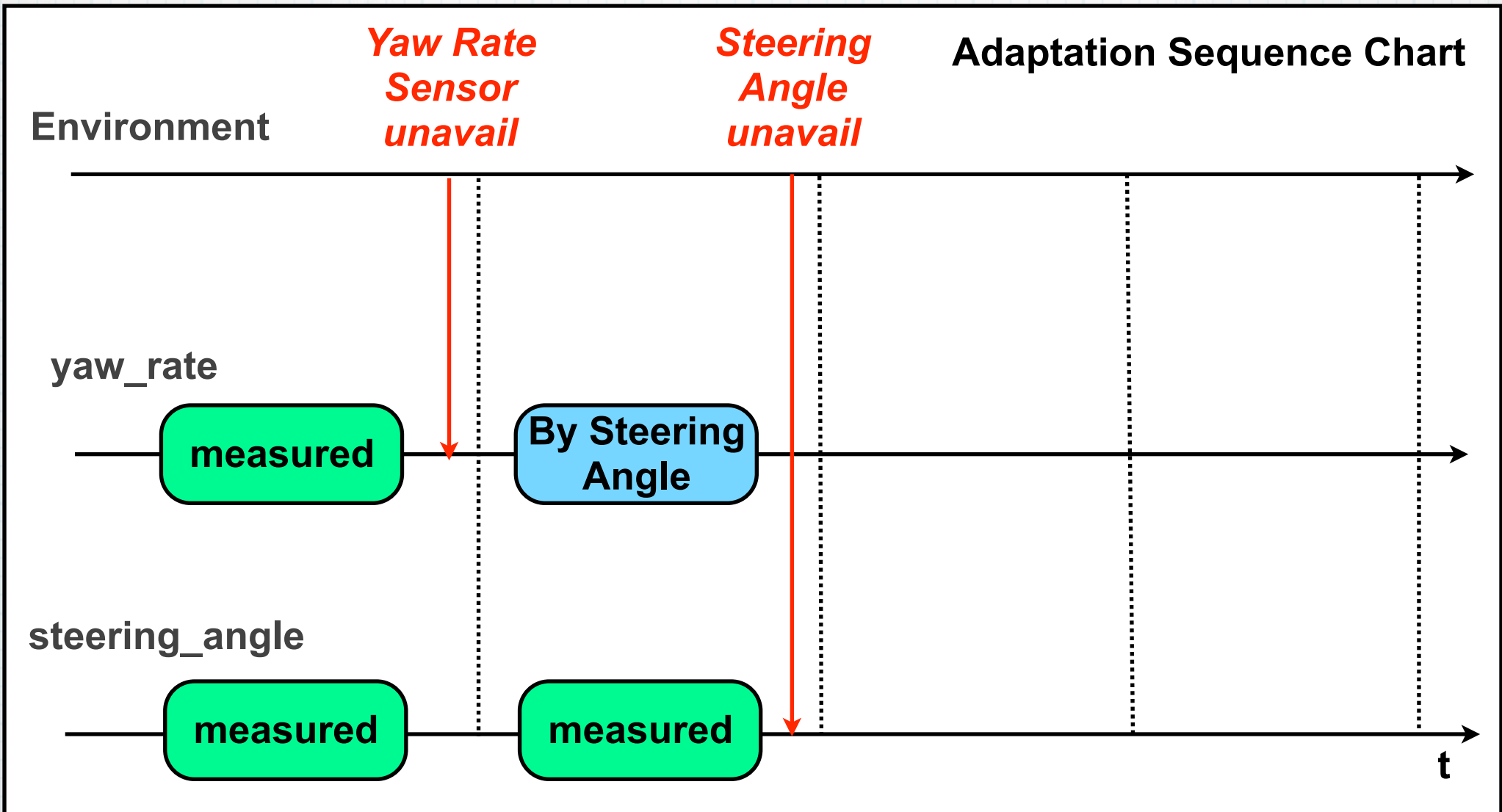
# Modelling Adaptation



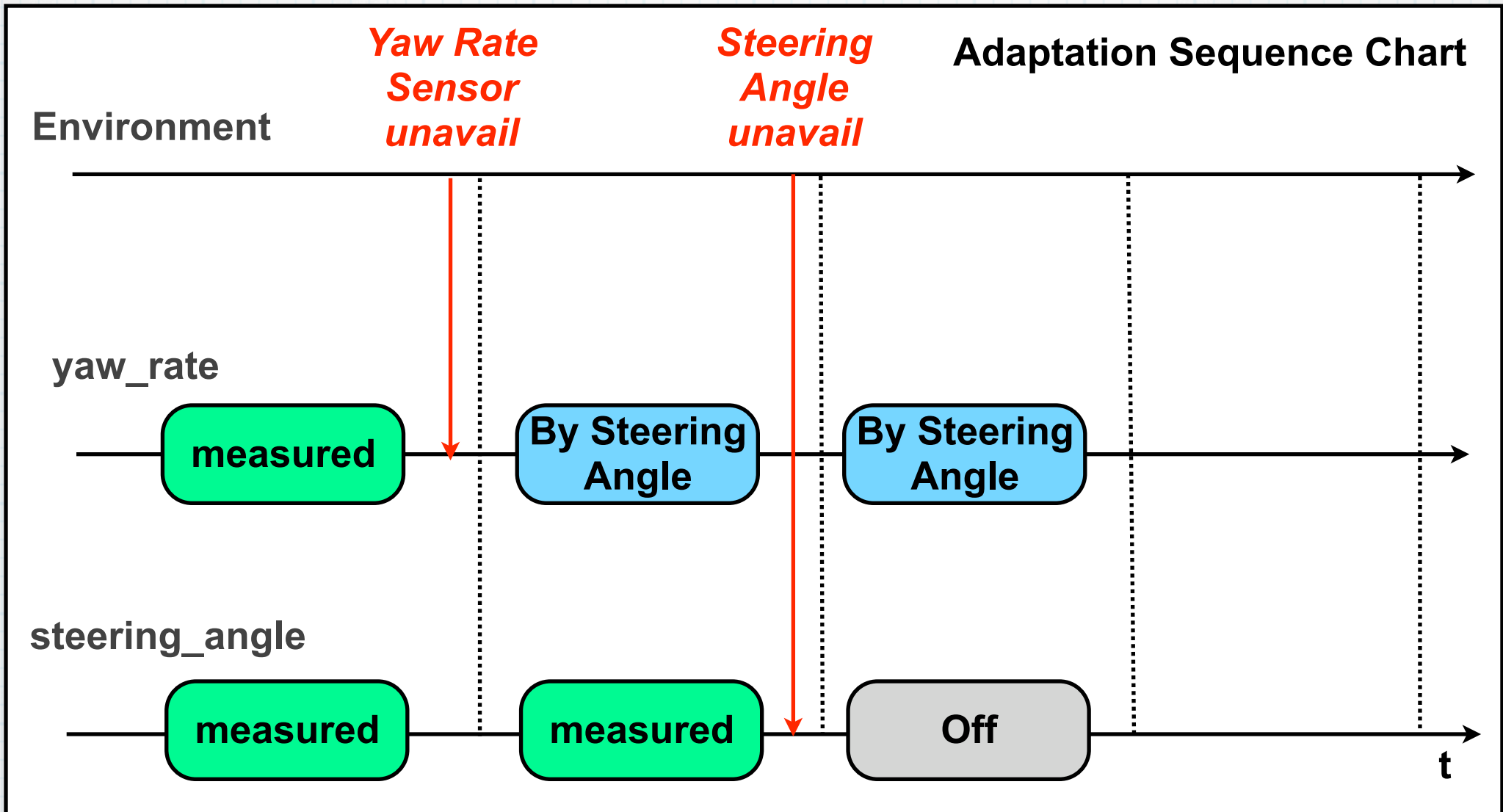
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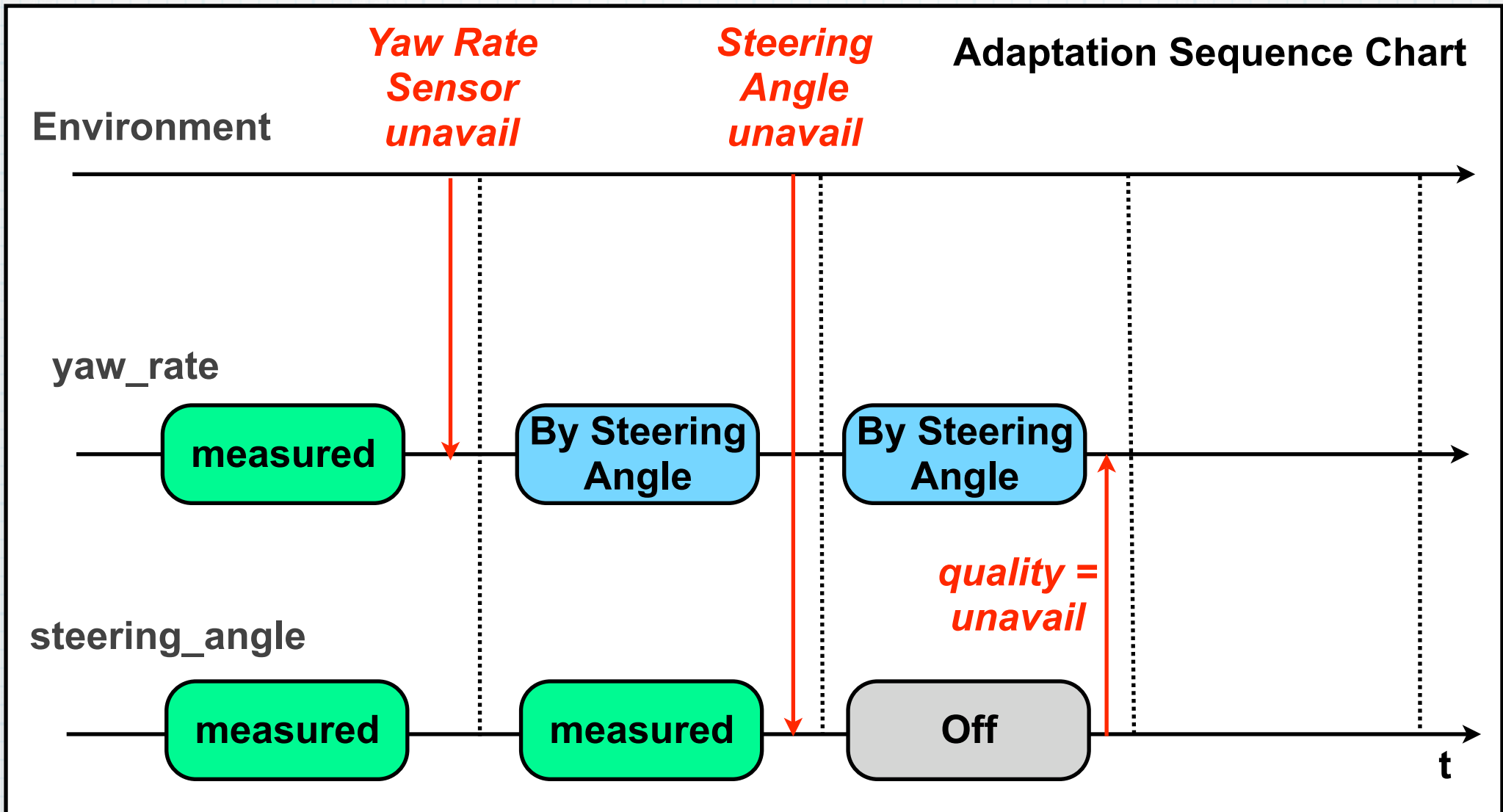
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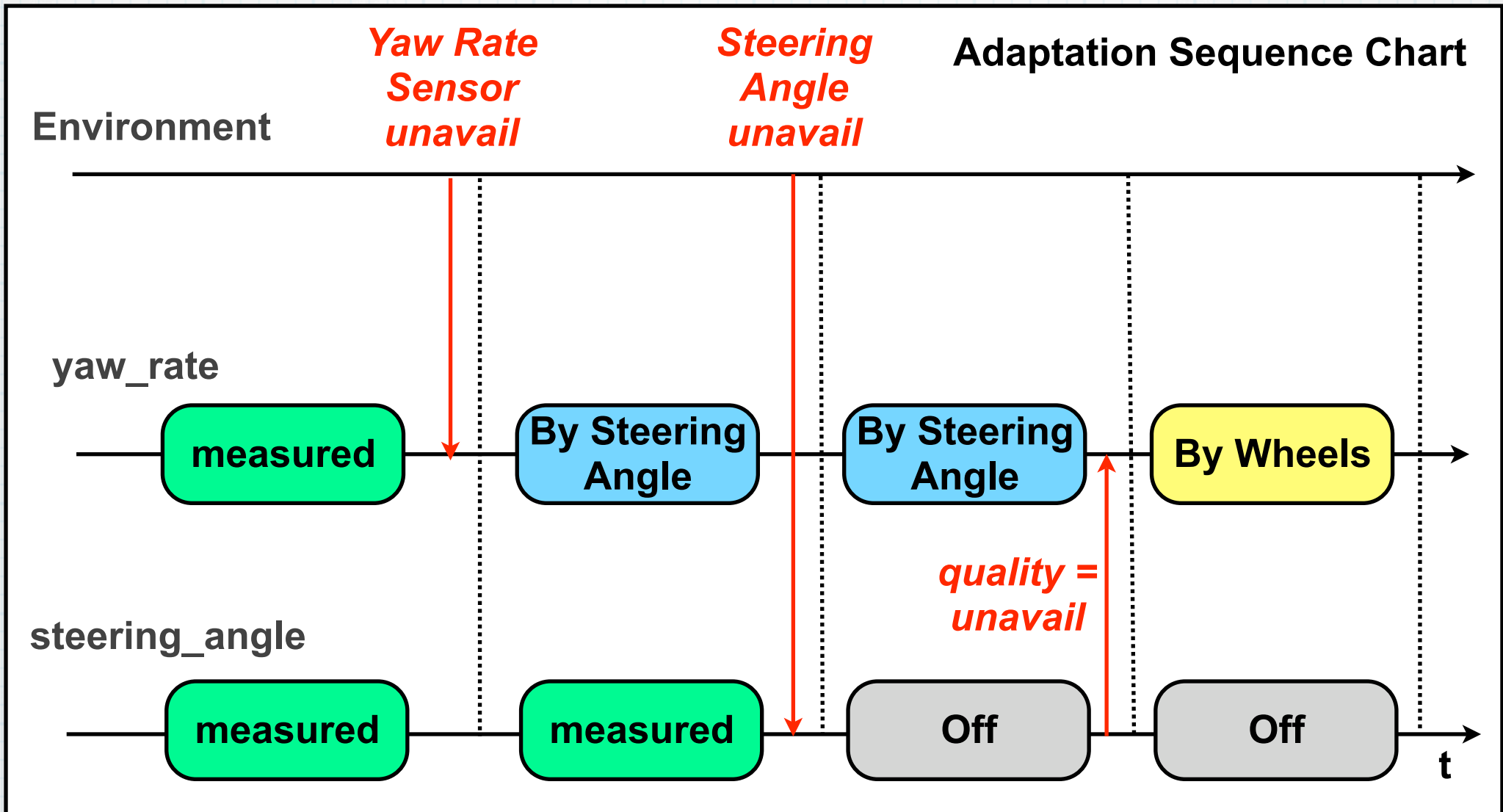
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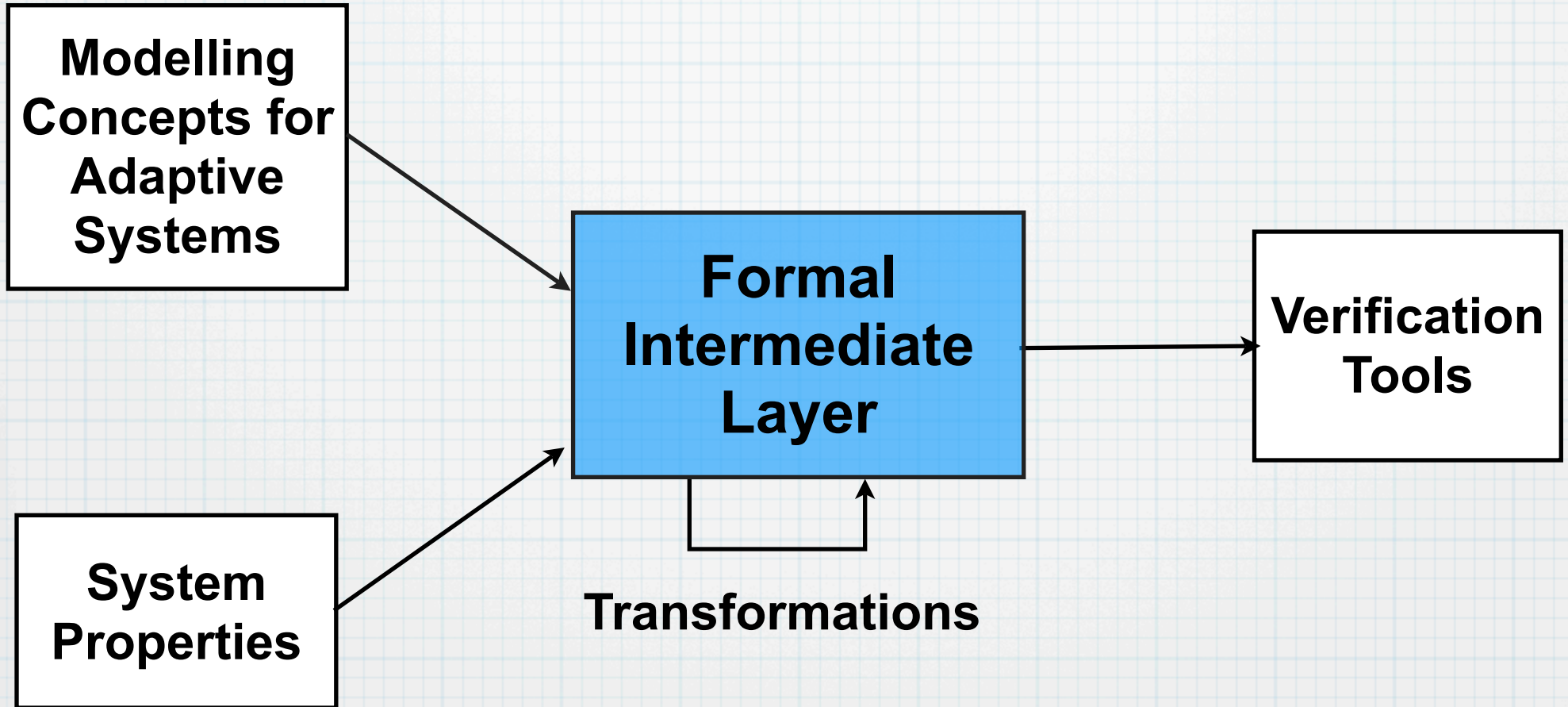


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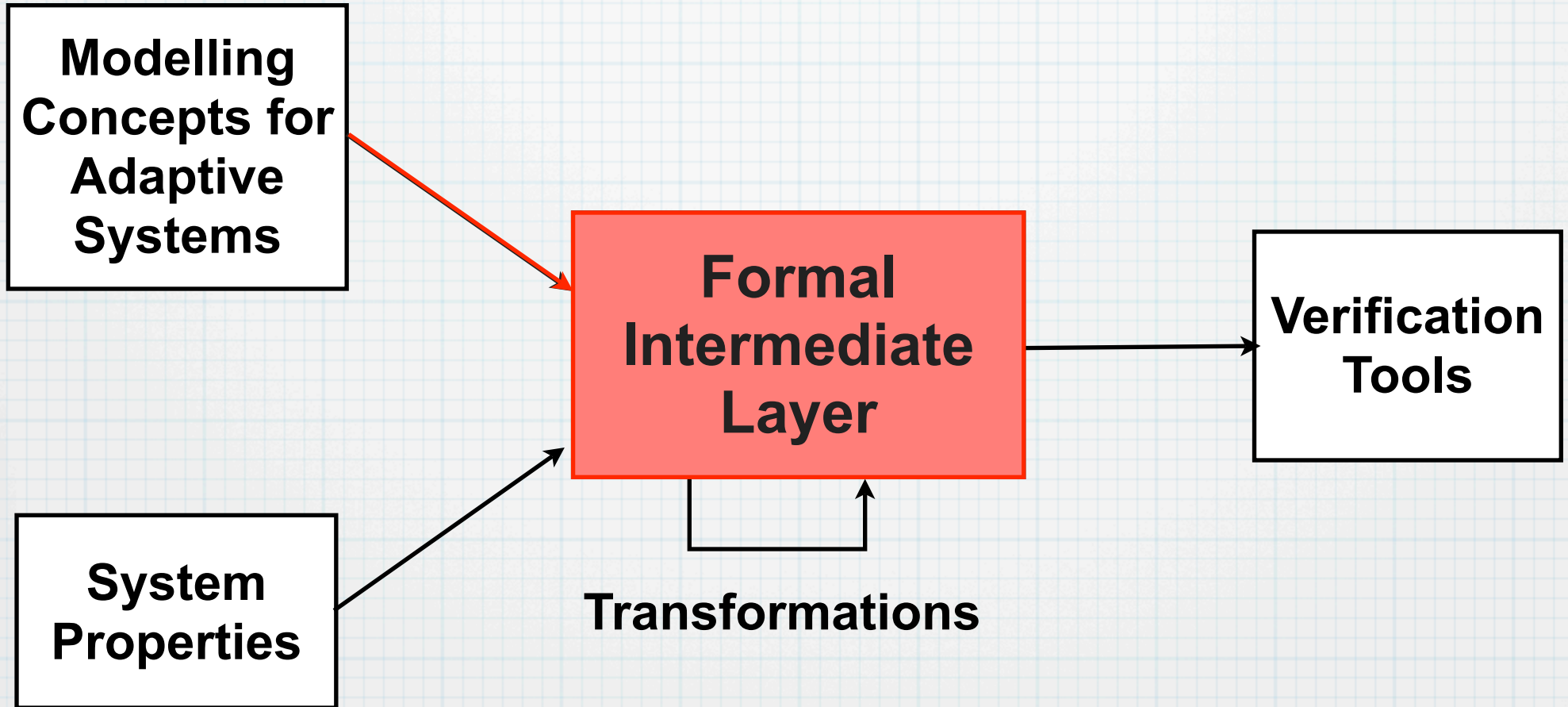
# Integration - Outline

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# Integration - Outline

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# Synchronous Adaptive Systems

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## Design Goals:

- \* **Modular System Structure**
- \* **Explicit and Separated Modelling of Adaptation and Functionality**
- \* **Formal Mathematical Model**

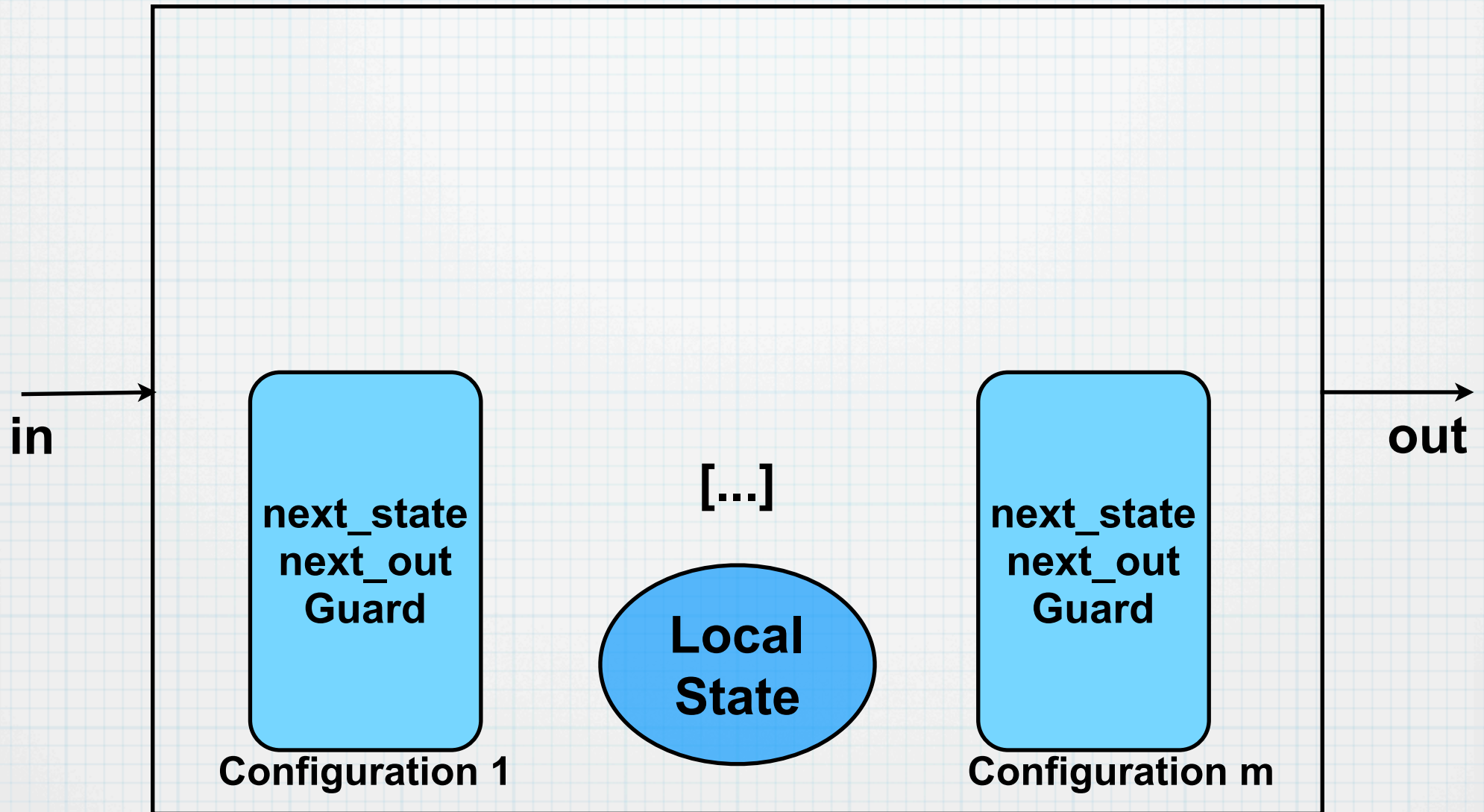
## Main Concepts:

- \* **Based on State-Transition Systems**
- \* **Uses Adaptation Aspect**

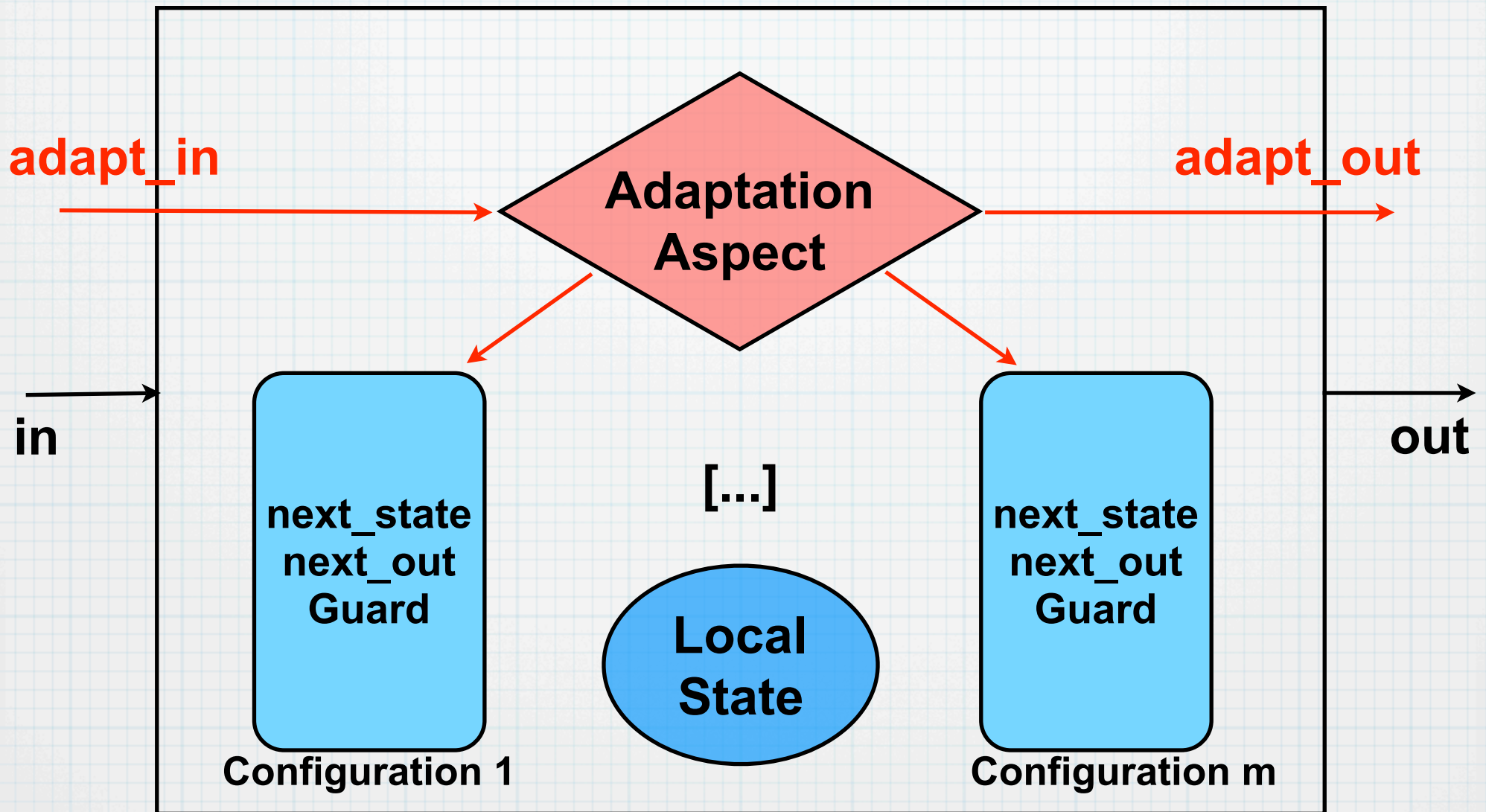
# SAS Module

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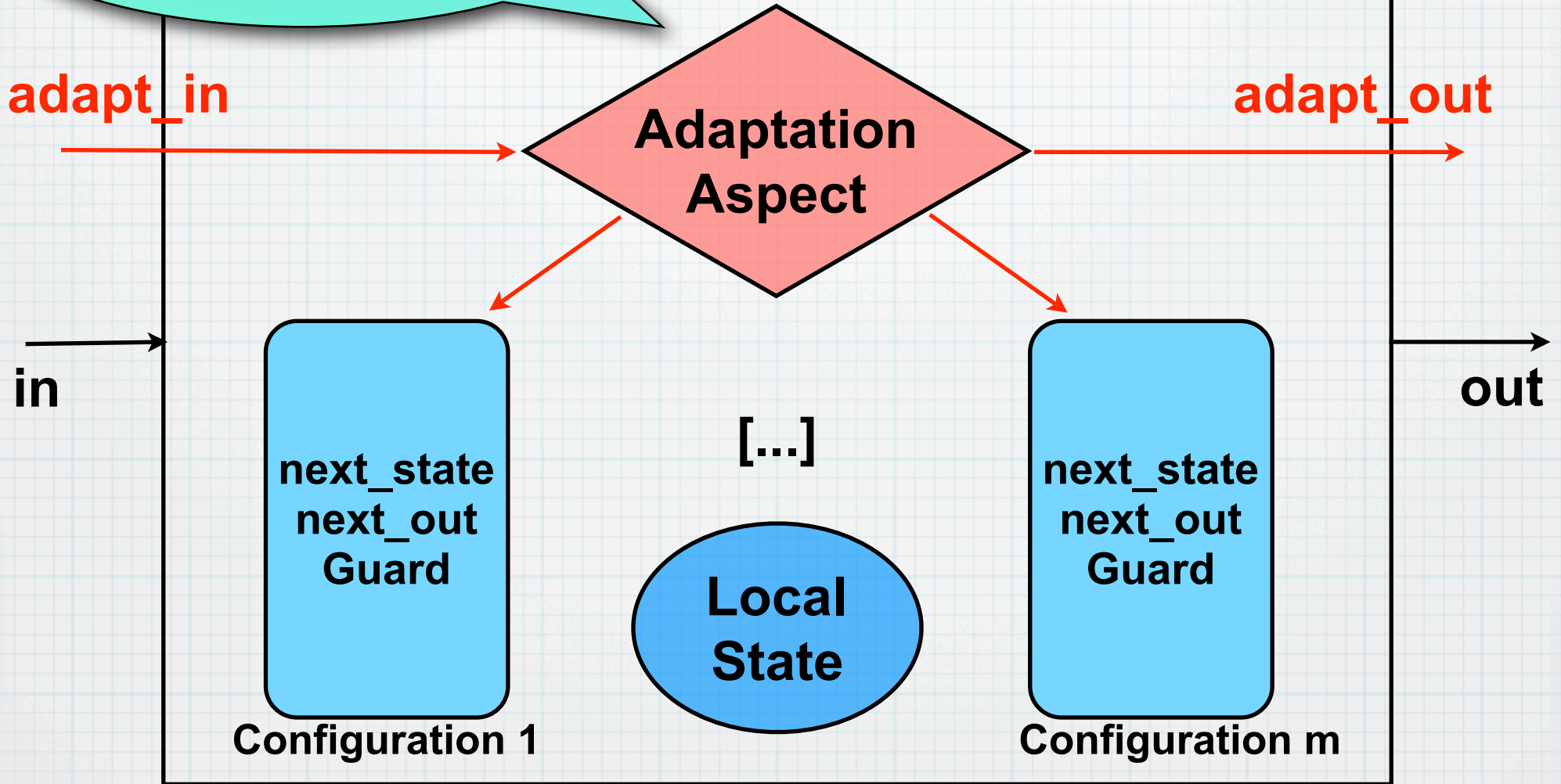


# SAS Module



# DAS Module

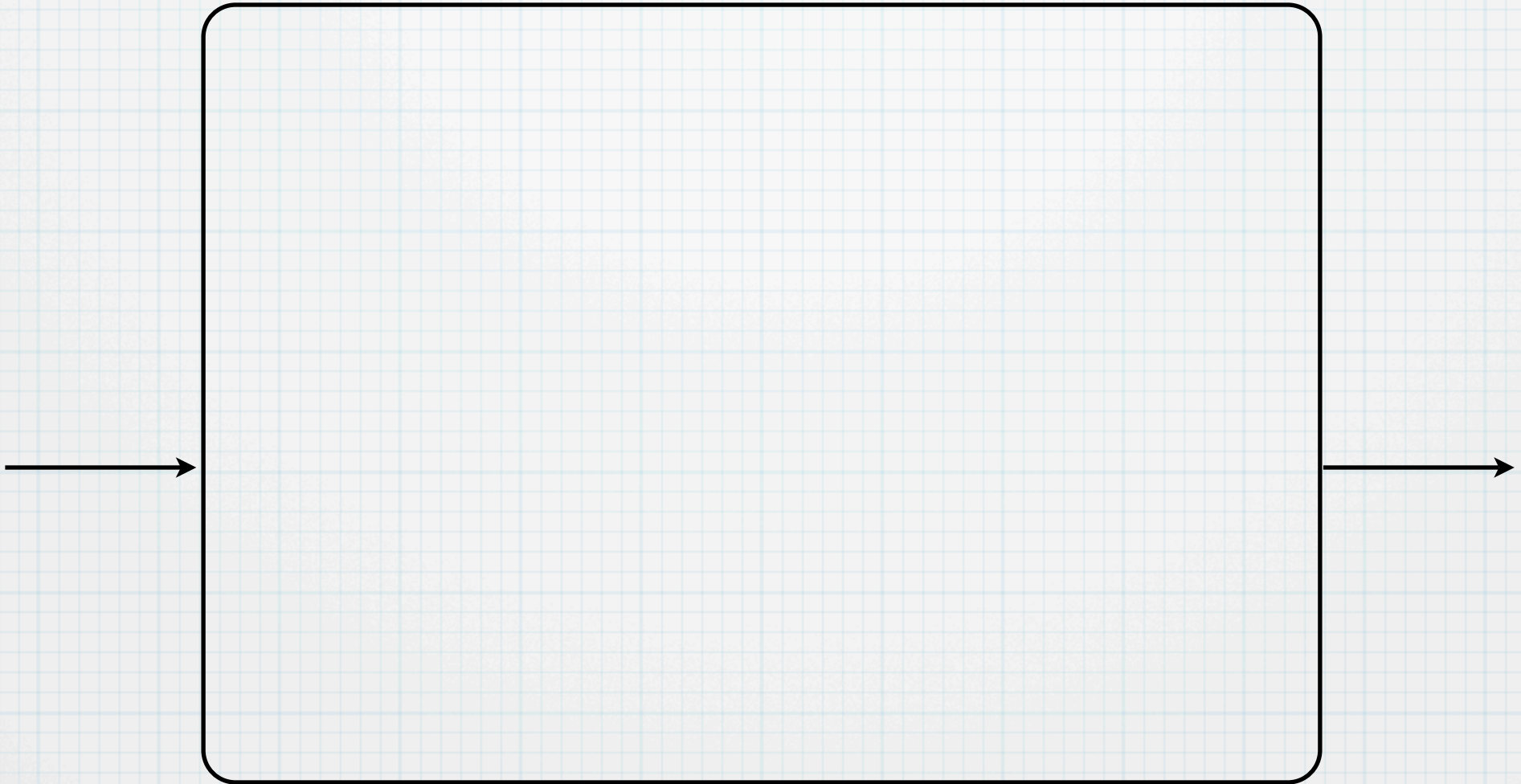
Independent  
Modelling of Functionality  
and Adaptation



# Traction Control System

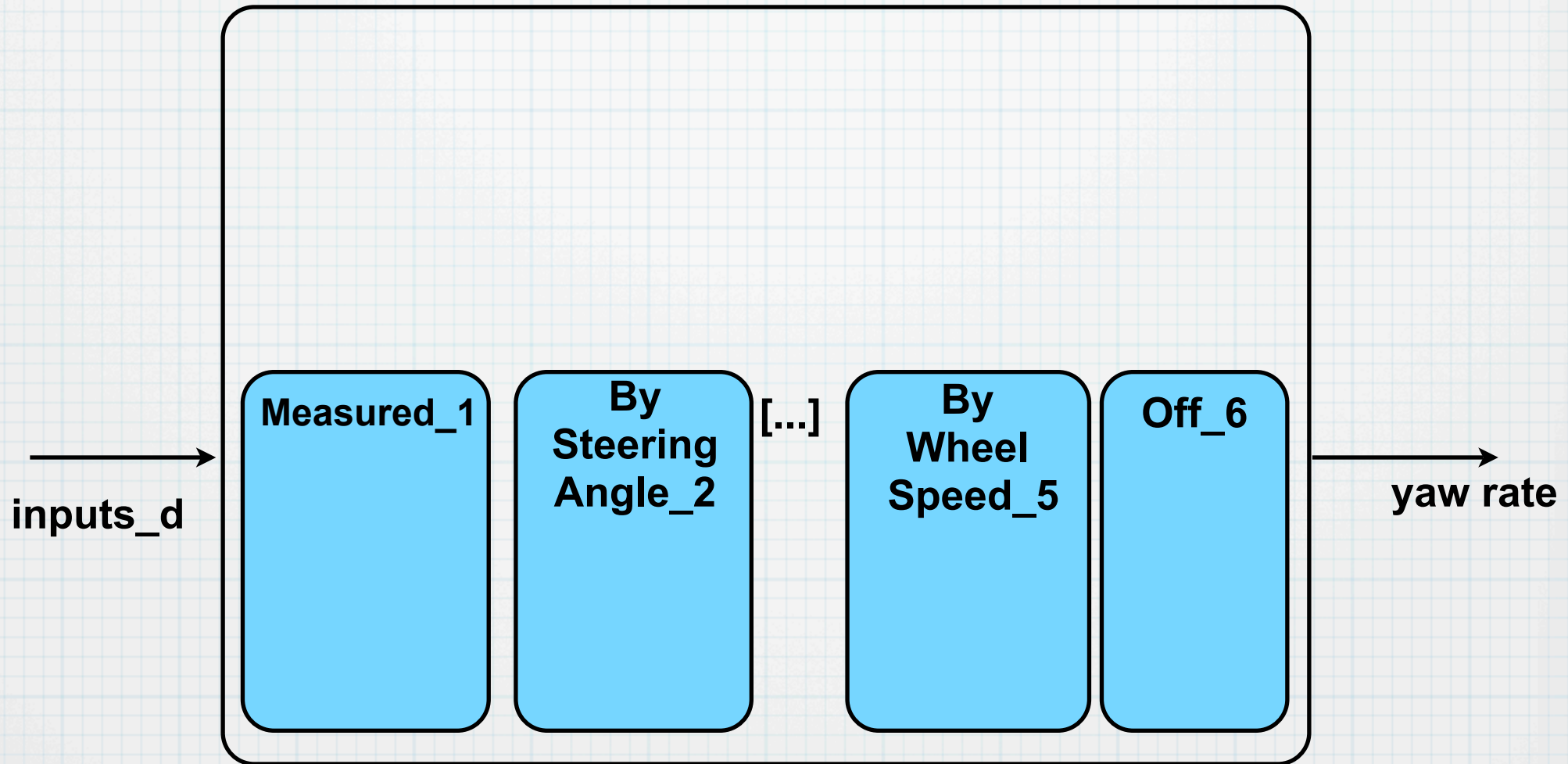
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## Example: Yaw Rate Module



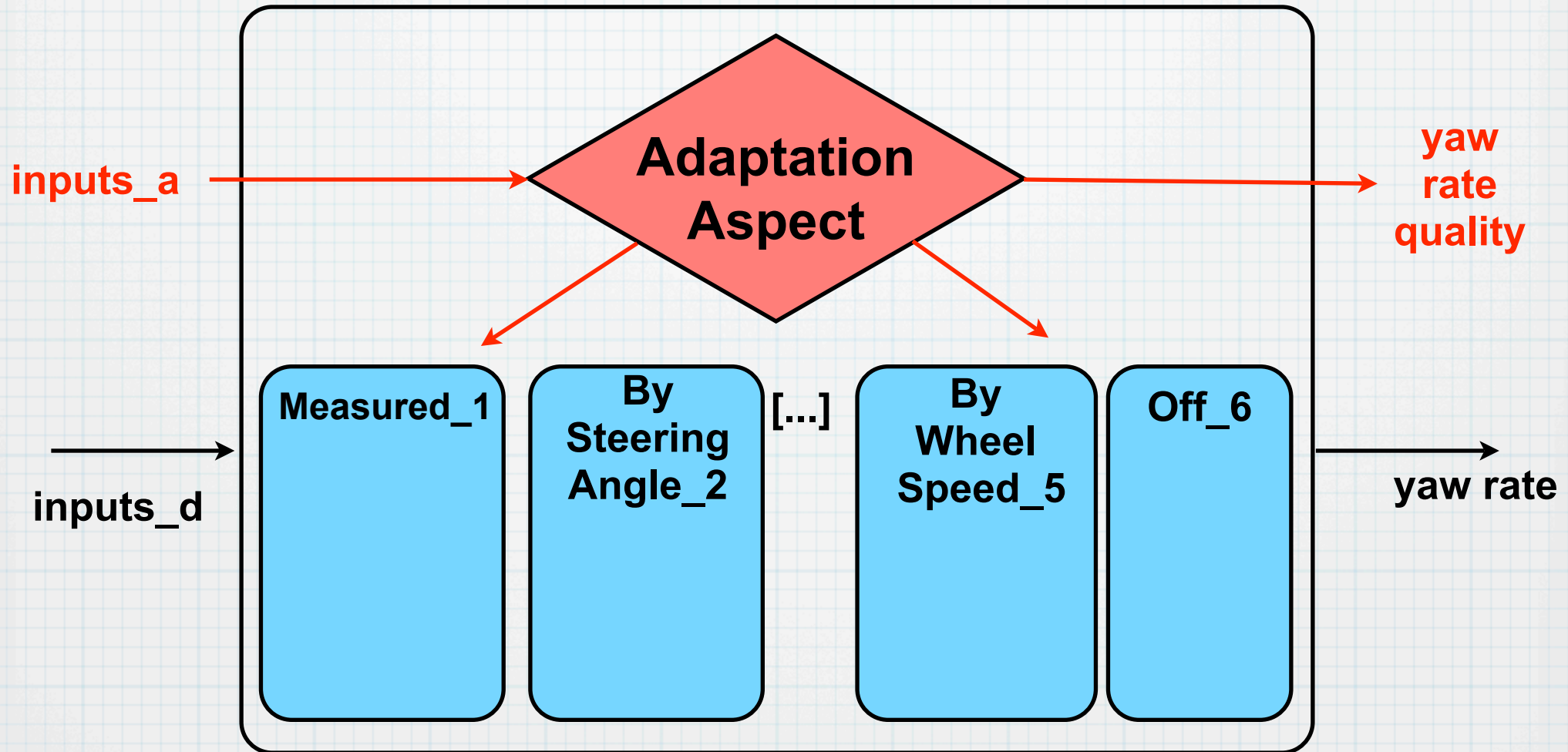
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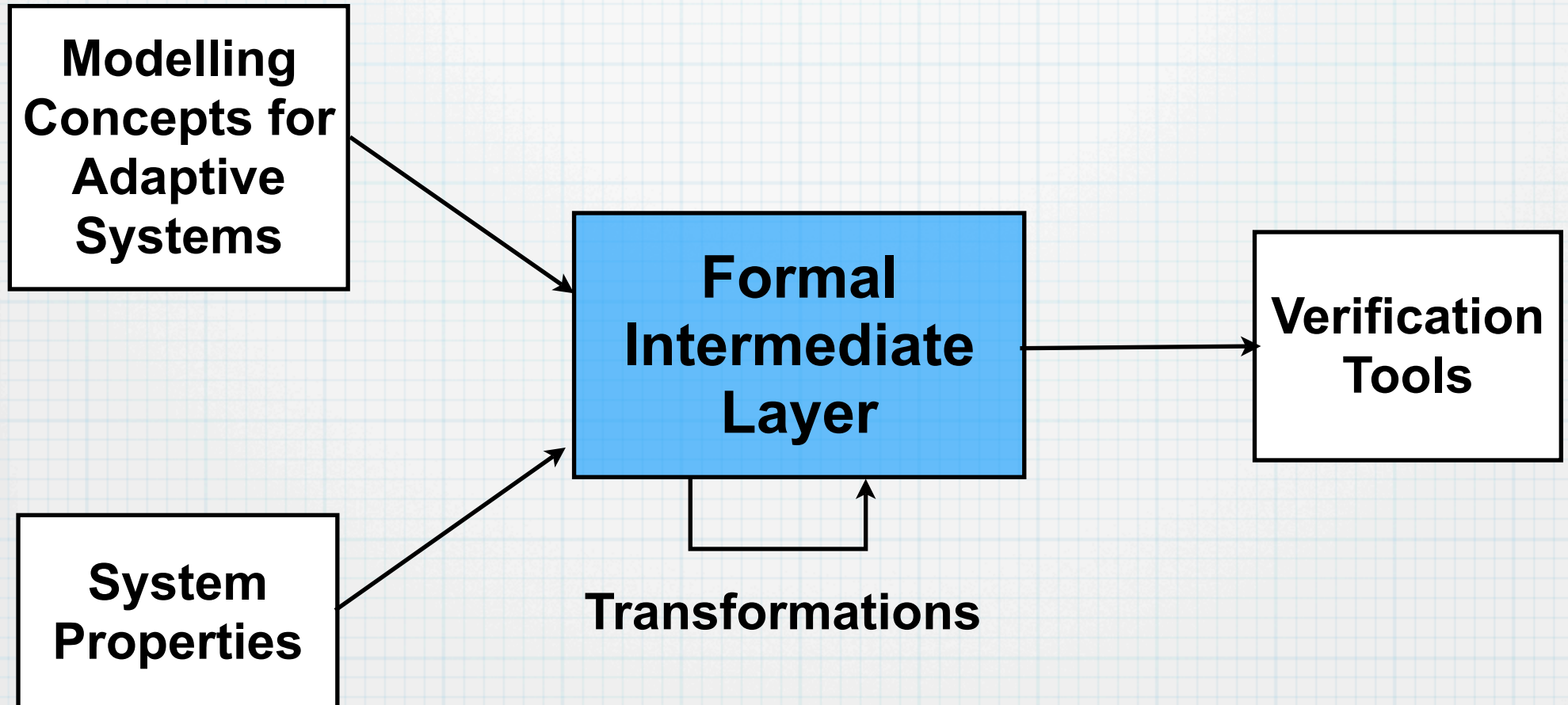
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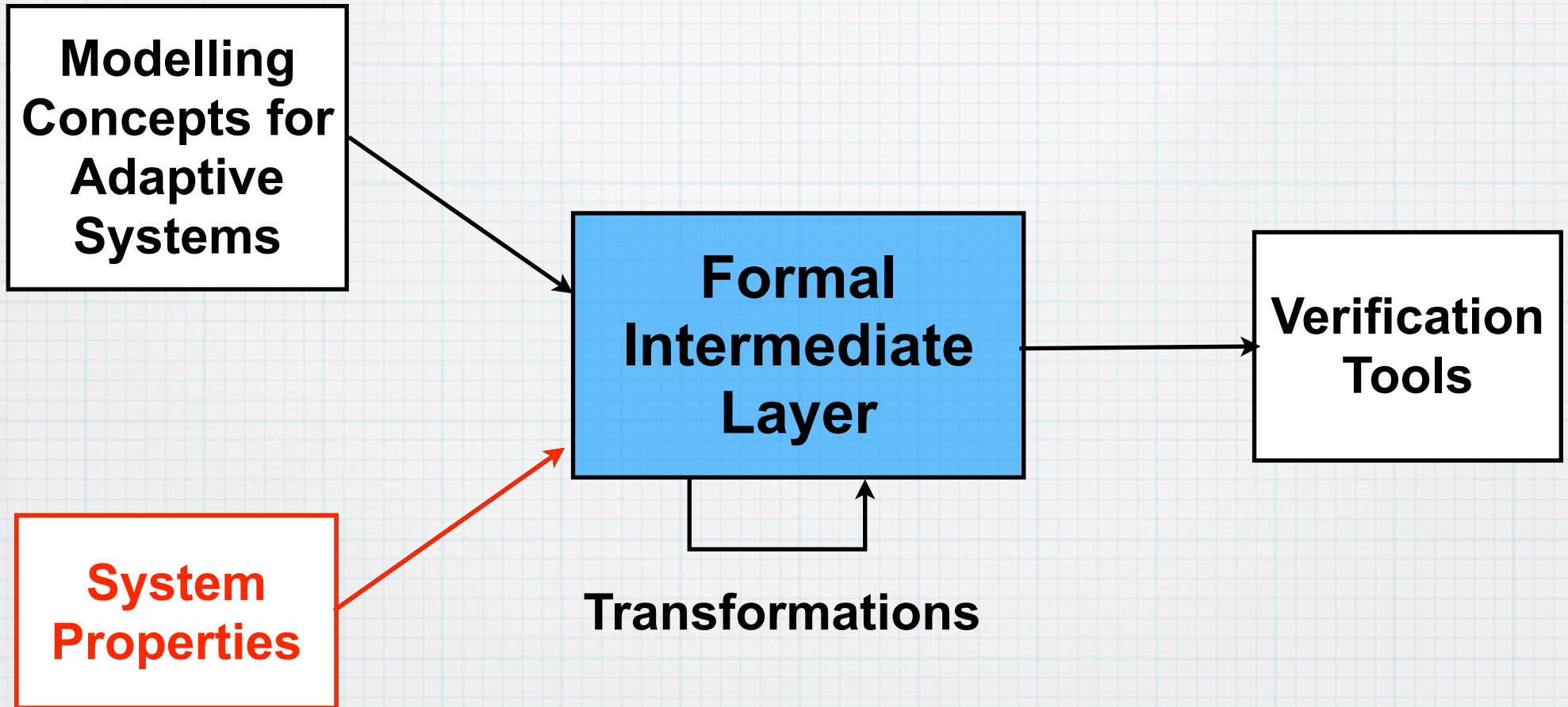
# Integration - Outline

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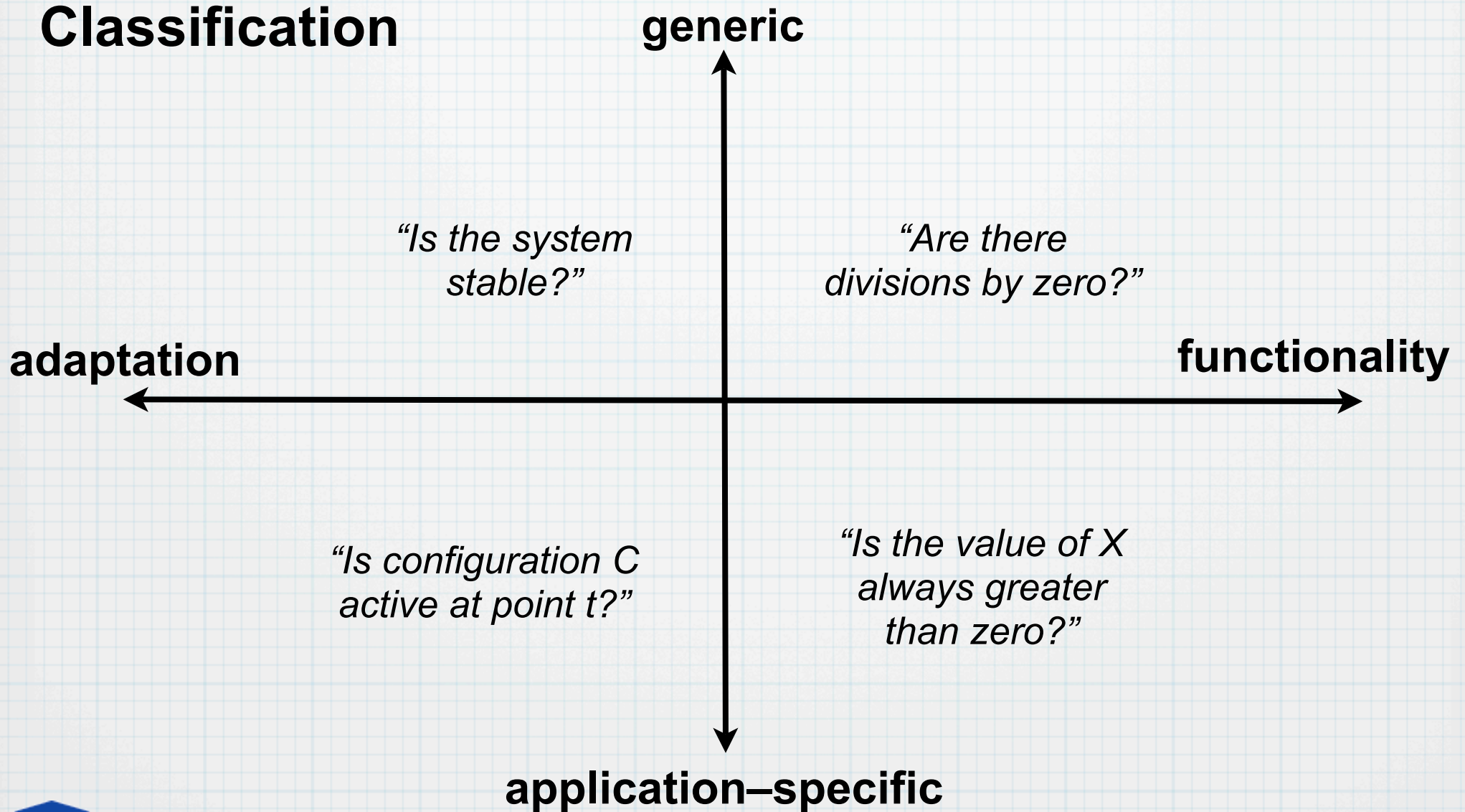
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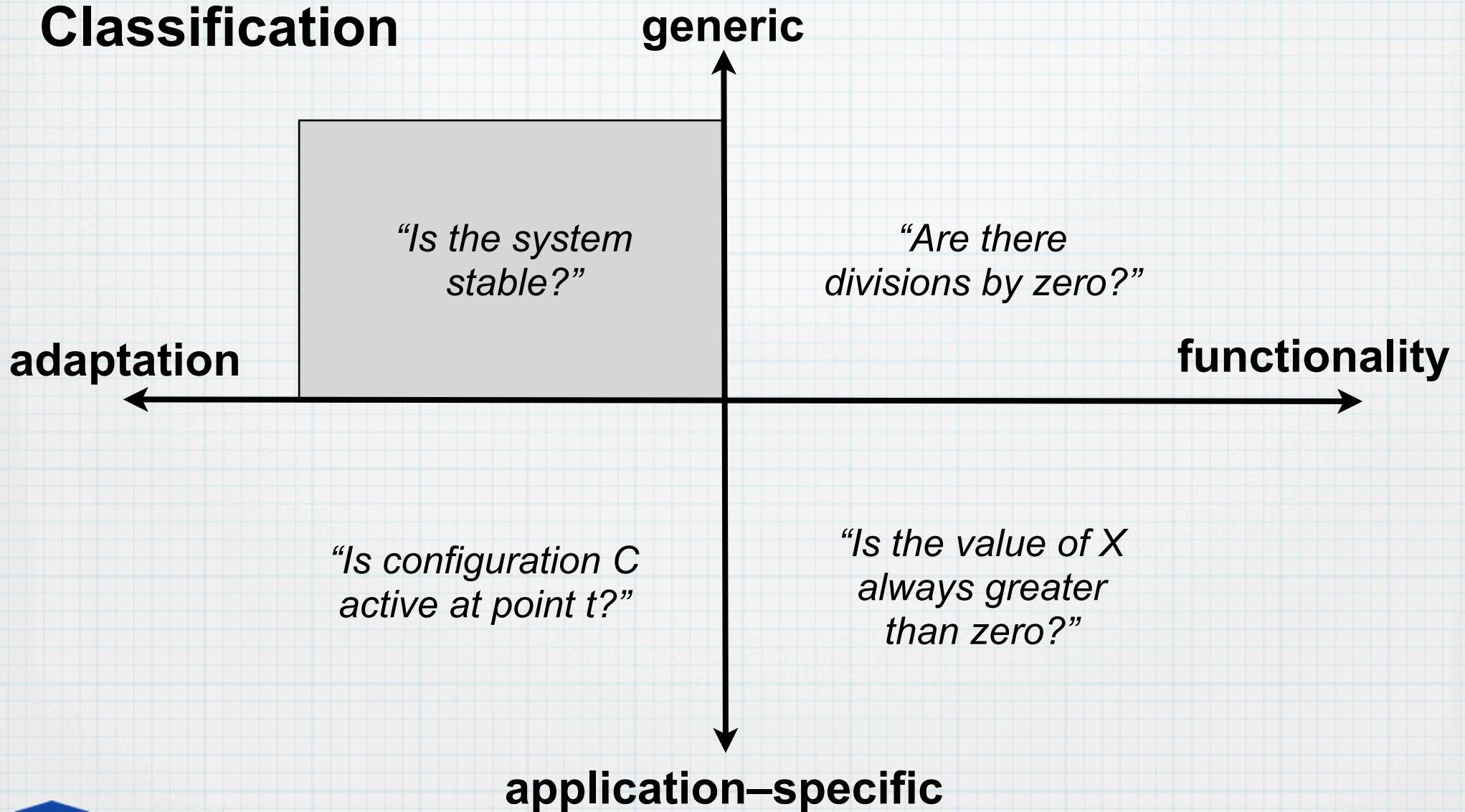
# System Properties

## Classification



# System Properties

## Classification



# Adaptive Generic Properties

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- \* No module gets stuck in the default configuration 'off':

$$AG(c = \text{off} \rightarrow EFc \neq \text{off})$$

- \* Every module can reach all configurations at all times:

$$AG\left(\bigwedge_{i=1}^n EF c = \text{config}_i\right)$$

- \* No inconsistent states can be reached:

$$AG\left(\bigvee_{i=1}^n c = \text{config}_i\right)$$

- \* No configuration is always only transient:

$$\bigwedge_{i=1}^n EFEG c = \text{config}_i$$

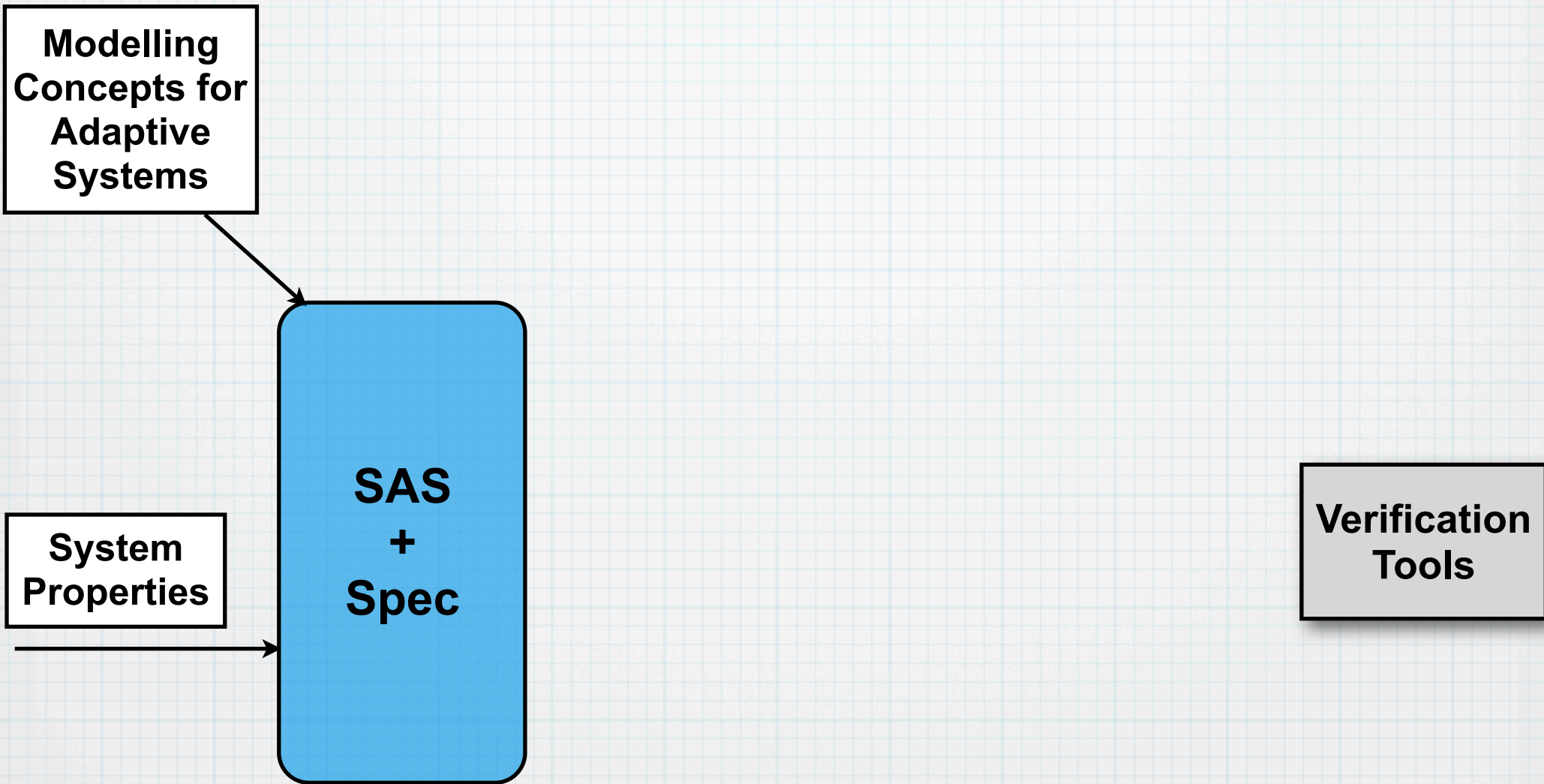
# Integration Framework

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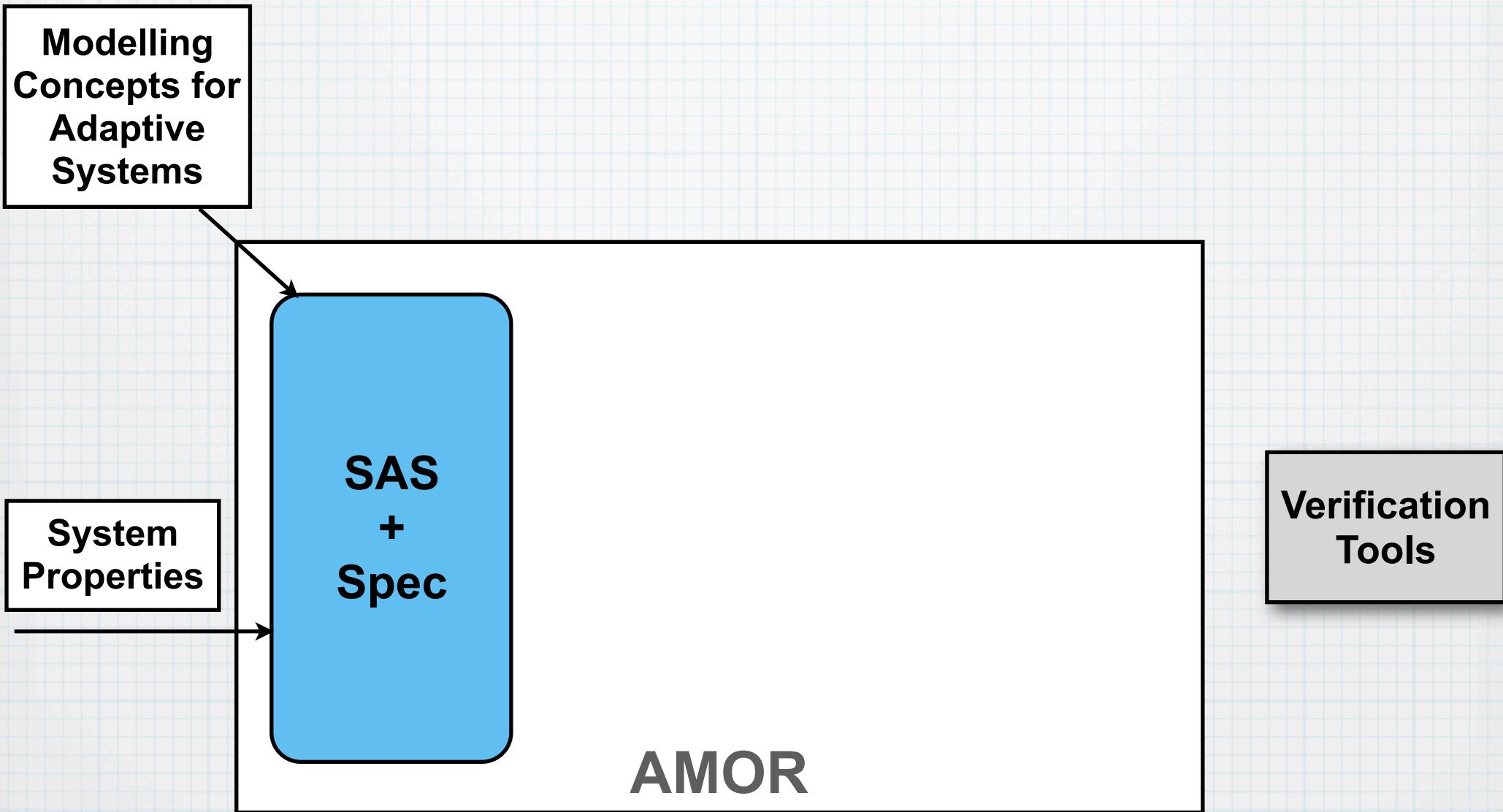
**Modelling  
Concepts for  
Adaptive  
Systems**

# Integration Framework

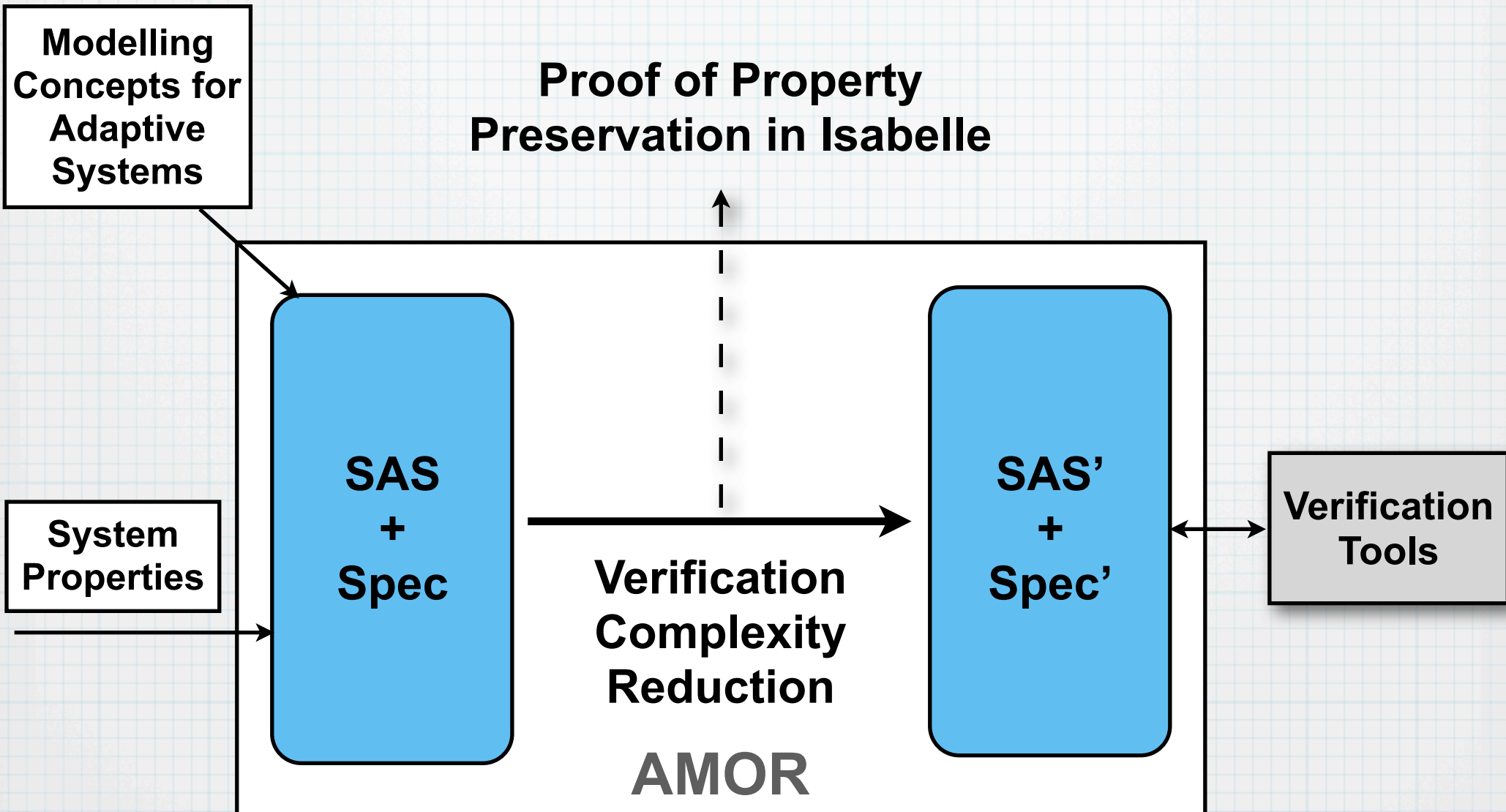
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# Integration Framework



# Integration Framework



# Verification Complexity Reductions

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- \* **Reductions by Slicing**
- \* **Data Domain Abstractions**
- \* **Compositional Reasoning**

# Stabilisation of Adaptation

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If input is unchanged, configurations will stabilise.

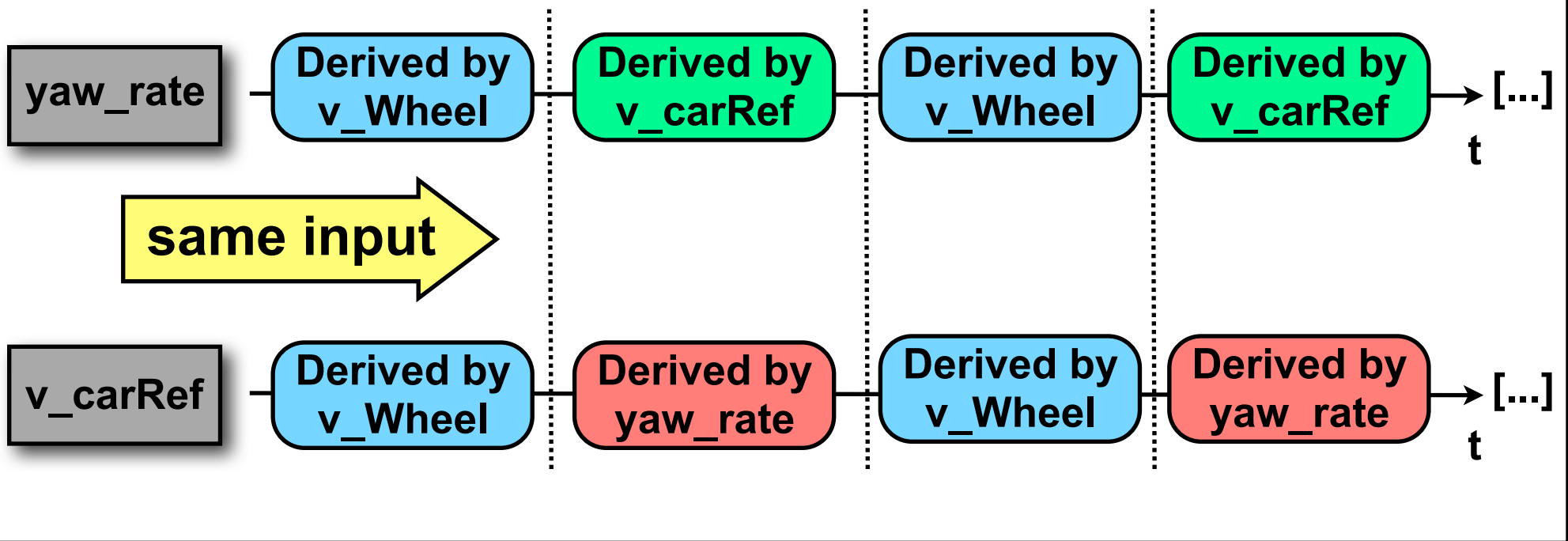
**AG( G same\_inputs => F G same\_configurations)**

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**AG( G same\_inputs => F G same\_configurations )**

Adaptation Sequence Chart



# Verification of Stability

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## \* Alternative Procedure:

Analyse two systems with one independent fixpoint each

1. Original System  $\triangleright$  set of reachable states
2. System restricted to input steady paths without self-loops  
 $\triangleright$  set of states with an infinite path (outputs not steady)

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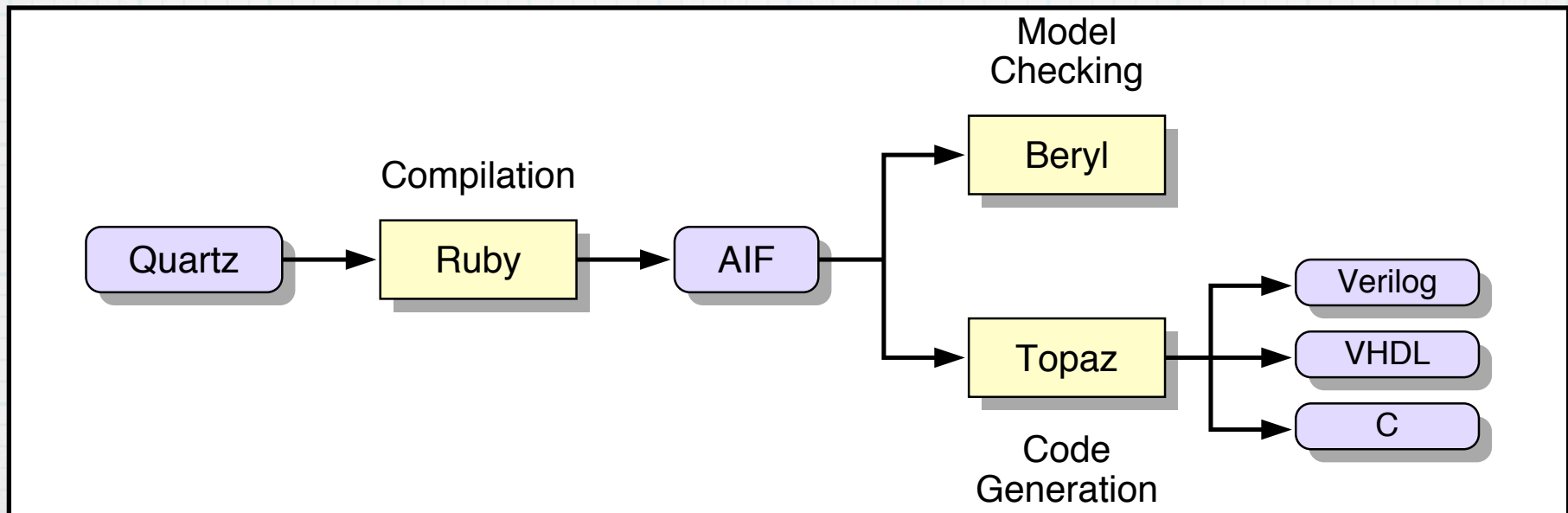
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**Theorem: Original system is stable iff intersection is empty!**

# Verification with AVEREST

- \* Framework for the development of reactive systems
- \* Quartz: synchronous language for describing parallel, deterministic systems
- \* Process communication and synchronisation part of the language



# Experimental Results

## Traction Control System:

28 modules, 70 configurations, > 2000 lines of Quartz code  
151 generic adaptation properties

*Generic specifications of adaptation behaviour*

event variables	min. [s]	avg. [s]	max. [s]	total [s]
no	< 1	5	222	782

*Stability of adaptation behaviour*

**LTL model checking: > 1h**

**Specialised procedure: ~0.48h**

# Related Work

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## Modelling and Verification of Adaptive Systems

- \* [Bradbury et al.; 2004]:  
Survey on Self-Managed Software Architectures
- \* [Zhang, Cheng; 2005/06]:  
Modelling and Verification of Adaptation Behaviour based on Petri Nets
- \* [Schneider, Schüle, Trapp; 2006]:  
Direct Translation of Modelling Concepts to Verification Tools

# Conclusion

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## Main Results:

- \* **Modelling Concepts for Adaptive Systems**
- \* **Framework for Integration of Model-based Design and Formal Verification using with High-Level Formal Model and Automatic Transformations for Complexity Reduction**
- \* **Standard and Specialised Verification Techniques for Adaptive Systems**

# Future Work

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- \* **Extension of Modelling Concepts with Intuitive Property Specification at Modelling Level**
- \* **Further Development of Reduction and Verification Techniques**
- \* **Propagation of Verification Results to Modelling Level**